# Stata Technical Bulletin

A publication to promote communication among Stata users

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stata54	Multiple curves plotted with stcurv command	
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Mario Cleves, Stata Corporation, mcleves@stata.com

Abstract: Stata's stcurv command which is used after streg to plot the fitted cumulative hazard, survival, and hazard functions, has been modified so that multiple curves can be plotted on the same graph.

Keywords: parametric survival, survival models, regression.

stcurv has been modified so that multiple curves can be plotted on the same graph. This is done by specifying multiple options, at1(), at2(), ..., one for each curve to be plotted.

#### Syntax

```
stcurv |, cumhaz survival hazard range(##)
```

[at1(varname=# [varname=#...]) [at2(varname=# [varname=#...]) [...]]]

graph\_options

The multiple at1(), at2(), ..., options are new. See [R] streg for a description of the other options.

stcurv is used after streg to plot the cumulative hazard, survival, and hazard functions at the mean value of the covariates or at values specified by the at() options.

#### New options

at1(varname=# ...), at2(varname=# ...), ..., at10(varname=# ...) specify that multiple curves (up to ten) are to be
plotted on the same graph. at1(), at2(), ..., at10() work like the at() option: the option causes the function to be
evaluated at the value of the covariates specified and at the mean of all unlisted covariates. at1() specifies the values of
the covariates for the first curve, at2() specifies the values of the covariates for the second curve, and so on.

Up to ten at() options can be specified at one time. Each at() option produces a separate curve on the same graph.

#### Example

We demonstrate the use of the multiple at() options by fitting a log-logistic regression model to the cancer data distributed with Stata, and plotting several predicted survival curves at various covariate values. For this example, we combine drug==2 and drug==3 into one group.

```
use cancer, clear
(Patient Survival in Drug Trial)
. replace drug=2 if drug==3
(14 real changes made)
. stset studytim, failure(died)
 (output omitted)
. streg age drug, dist(llog) nolog
       failure _d: died
  analysis time _t: studytim
Log-logistic regression -- accelerated failure-time form
No. of subjects =
                     48
                                         Number of obs
                                                               48
No. of failures =
                       31
Time at risk
                      744
                                          LR chi2(2)
                                                       =
                                                            35.14
Log likelihood =
                -43.21698
                                          Prob > chi2
                                                            0.0000
  _____
    _t | Coef. Std. Err. z P>|z| [95% Conf. Interval]
                   _____
   age -.0803289 .0221598 -3.625 0.000
                                            -.1237614 -.0368964
  drug | 1.420237 .2502148
_cons | 5.026474 1.225037
                            5.676 0.000
4.103 0.000
                                                .9298251
                                                          1.910649
                                                2.625446
                                                          7.427502
                               _ _ _ _ _ _ _ _ _
/ln_gam | -.8456552 .1479337 -5.716 0.000
                                                -1.1356 -.5557104
_____
           _____
                   _____
                                                -----
                                                         _____
  gamma .429276 .0635044
                                                .3212293 .5736646
```



We first obtain a graph with two predicted survival curves, one for each drug treatment group, at the overall average age.



Figure 1. Predicted survival curves for drug treatment groups at overall average age.

We specified two at() options, one for each drug group. Now let's plot the two treatment groups, not at the average patient age, but, for example, at age 40.

. stcurv, survival at1(drug=1 age=40) at2(drug=2 age=40) c(ll) xlab ylab



Figure 2. Predicted survival curves for drug treatment groups at age 40.

Again we specified at () twice, but now we included age=40 in each option's argument. We could include additional curves in the graph; for example, to the previous graph we now add two more curves each at age 65.

> . stcurv, survival at1(drug=1 age=40) at2(drug=2 age=40) at3(drug=1 age=65) > at4(drug=2 age=65) c(1111) xlab ylab

> > (Graph on next page)



Figure 3. Predicted survival curves for drug treatment groups at ages 40 and 65.

stata55	Search web for installable packages			
		*****		110

William Gould, Stata Corporation, wgould@stata.com Alan Riley, Stata Corporation, ariley@stata.com

Abstract: webseek searches the web for user-written additions to Stata, which is to say, new commands. The search includes but is not limited to additions published in the STB. The commands found are available for immediate installation using the net command or, under Windows and Macintosh, by clicking on the link shown in webseek's output. webseek can find additions based on topic, author name, or the command name.

Keywords: search, net, web, user-written additions, programs, commands.

#### Syntax

webseek keywords , or nostb tocpkg toc pkg everywhere filenames help result type errnone

## Description

webseek searches the web for user-written additions to Stata, which is to say, new commands. The search includes, but is not limited to, additions published in the STB.

The commands found are available for immediate installation using the net command or, under Windows and Macintosh, by clicking on the link shown in webseek's output. webseek can find additions based on topic, author name, or the command name.

#### Options

- or is relevant only when multiple keywords are specified. By default, only packages that include all the keywords are listed. or changes this to list packages that contain any of the keywords.
- nostb restricts the search to non-STB sources or, said differently, causes webseek not to list matches that were published in the STB.
- tocpkg, toc, and pkg determine what is searched. tocpkg is the default, meaning that both table of contents (tocs) and packages (pkgs) are searched. toc restricts the search to table of contents only. pkg restricts the search to packages only.
- everywhere and filenames determine where in packages webseek looks for keywords. The default is everywhere. filenames restricts webseek to search for matches only in the filenames associated with a package. Specifying everywhere implies pkg.
- help, result, and type determine how and where results are displayed.

help specifies that results are to be displayed in the help window, where you can point and click to visit the links. help is the default with Stata for Windows and Stata for Macintosh. help may not be specified with Stata for Unix (because there is no help window).

result specifies that results are to be displayed in the standard Stata results window. result is the default with Unix but the option may be specified with Windows or Macintosh.

type is the default on no platform but may be specified on all. It presents output much like result, but without highlighting. Its advantage is that the results of a search can be logged.

In addition, you may set the global macro \$webseek to contain help, result, or type and so specify your own default.

errnone is an option for programmers using webseek as a subroutine. It causes the return code to be 111 rather than 0 when no matches are found.

## Remarks

Not just we at Stata, but others can write new commands for Stata, so if Stata cannot do something it may be that someone has written an addition to do it. The problem is finding that addition.

webseek searches the web for net-installable additions to Stata. net (see [**R**] net) is the Stata command that can install new additions to Stata. If you knew, for instance, that a user A. Smith wrote an addition you wanted and that it was available as package veryneat at http://www.university.edu/~asmith, you could type

```
. net from http://www.university.edu/~asmith
. net install veryneat
```

and then you would have the veryneat command. Probably A. Smith provided a help file to go with the new command, so typing help veryneat should now tell you something about how to use this new command. Eventually, you would discover that command veryneat was very useful or it was not worth the disk space it occupied. If the latter, you could type

. ado uninstall veryneat

and so remove it from your computer.

The problem is in finding the veryneat command in the first place. webseek helps with that.

#### Example 1: Find what is available about "random effects"

```
. webseek random effect
```

Comments:

- 1. It is best to search for the singular. 'webseek random effect' will find both "random effect" and "random effects".
- 2. 'webseek random effect' will also find "random-effect" (note the hyphen) because webseek performs a string search, not a word search.
- 3. 'webseek random effect' lists all packages containing the words "random" and "effect", not necessarily used together.
- If you wanted all packages containing the word "random" or the word "effect", you would type 'webseek random effect, or'.

#### Example 2: Find what is available by author Jeroen Weesie

. webseek weesie

Comments:

- 1. You could type 'webseek jeroen weesie' but that might list less because perhaps the last name is used without the first.
- 2. You could type 'webseek Weesie' and that would produce the same results. Capitalization, both in what you type and what is at the site, is ignored in the search.

#### Example 3: Same as example 2, but do not list STB materials

```
. webseek weesie, nostb
```

Comments:

- 1. The STB tends to dominate search results because so much has been published in the STB. If you know what you are looking for is not in the STB, specifying the nostb option will narrow the search.
- 2. 'webseek weesie' lists everything 'webseek weesie, nostb' lists, and more. If you just type 'webseek weesie', look down the list. STB materials are listed first and non-STB materials are listed after that.

## Example 4: Find the user-written command kursus

. webseek kursus, file

Comments:

- 1. You could just type 'webseek kursus' and that will list everything 'webseek kursus, file' lists, and more. Since you know kursus is a command, however, there must be a kursus.ado file associated with the package. Typing 'webseek kursus, file' narrows the search.
- 2. You could also type 'webseek kursus.ado, file' to narrow the search even more.

#### Where does webseek look?

webseek looks everywhere, not just at www.stata.com. webseek begins by looking at www.stata.com, but then follows every link, which takes it to other places, and it then follows every link, which takes it to yet more places, and so on.

Authors: please let us know if you have a site we should include in our search by sending email to webseek@stata.com. We will then link to your site from ours and so ensure that webseek finds your materials. That is not strictly necessary, however, as long as your site is linked from some site that is linked to ours, even if that link is indirect.

## How does webseek really work?



www.stata.com maintains a database of Stata resources. When you use webseek, webseek contacts stata.com with your request, stata.com searches its database, and returns the result to you.

Another part of the system is called the crawler: it searches the web for new Stata resources to add to the webseek database and it verifies that the resources already found are still available. Given how the crawler works, when a new resource becomes available, the crawler takes about two days to notice it and, similarly, if a resource disappears, the crawler takes roughly two days before it is removed from the database.

## Note

When you use webseek, it creates file wseekres.hlp in the current directory. If the file bothers you, you may erase it.

dm73.1	Contrasts for categorical variables: update

John Hendrickx, University of Nijmegen, Netherlands, J.Hendrickx@mailbox.kun.nl

Abstract: Bug fixes and enhancements to desmat and associated programs for models with categorical independent variables are described.

Keywords: Contrasts, interactions, categorical variables.

#### Changes to desmat

The program desmat can be used to create dummy variables for categorical variables using a variety of contrasts (Hendrickx 1999). This update corrects bugs in the original version and adds a minor enhancement. These bugs can occur if categorical variables have values other than their rank number, in which case dummies using the deviation, difference, or Helmert contrasts will be incorrect. It also turns out that orthpoly can produce errors if large values such as years are used. This problem has been reported and circumvented in desmat by subtracting the lowest value of the variable before calling orthpoly.

An enhancement to desmat is the option to assign a contrast to a variable by using a pzat characteristic. For example, to specify that the variable educ should be treated as continuous by desmat, use

. char educ[pzat] dir

The pzat characteristic overrides the default parameterization specified as an option to the desmat statement. For example:

```
. desmat educ focc, dif
```

desmat will treat educ as a continuous variable but will use the difference contrast for focc. This can also be achieved by appending =par[(ref)] to specific model terms; for example:

```
. desmat educ=dir focc, dif
```

Using the pzat characteristic can be more practical in large models where a specification per variable would become overly long. A specification per variable can be used to override the pzat characteristic. For example, specifying educ=sim(1) in the above statement will cause the simple contrast to be used for educ.

#### Changes to desrep

desrep can be used after estimating a model to produce an overview of the results using informative labels. It will now work properly with mlogit (the previous version stripped equation names from \_b() and \_se() when formatting the results). desrep will also print model results such as the procedure name, dependent variable, sample size, log likelihood, F-statistic, chi-square, etc. If certain e() macros have been defined by a procedure, they will be printed by desrep with a suitable label.

#### Replacement of tstall by destest

In Hendrickx (1999), tstall was provided to perform a Wald test on all model terms after estimating a model generated by desmat. An enhanced version renamed destest can now do tests on specific terms only. The syntax is

```
destest [termlist] [, equal joint ]
```

The *termlist* consists of one or more terms as specified in desmat. A term can consist of a single variable, or two or more variables separated by either asterisks or periods. If asterisks are used, they will be changed into periods by destest, that is, only the highest order interaction will be tested. This syntax makes it easier to copy the model syntax and test the highest order terms, which is what people will usually want to do. If destest is specified without any arguments, all terms from the last desmat model will be tested.

The default is to test whether the effects of each separate term are equal to zero. If the option joint is specified, destest will test instead whether all the effects in *termlist* are jointly equal to zero. If the option equal is specified, destest will test whether the effects of each separate term are equal. The joint and equal options may be combined to test whether all effects are jointly equal, although this would be a somewhat peculiar hypothesis.

## Reference

Hendrickx, J. 1999. dm73: Using categorical variables in Stata. Stata Technical Bulletin 52: 2-8.

#### dm76 ICD-9 diagnostic and procedure codes

William Gould, Stata Corporation, wgould@stata.com

Abstract: Two commands are provided for dealing with ICD-9 codes; icd9 for use with diagnostic codes and icd9p for use with procedure codes.

Keywords: ICD-9-CM diagnostic codes, ICD-9-CM procedure codes.

#### Completing the installation

The installation process for the icd9 and icd9p commands are a little different than the standard. In addition to net install, you must net get and then you must type icd9 install and icd9p install:

. net install dm76

. net get dm76

. icd9 install

. icd9p install

The net get copies two datasets that icd9 and icd9p need that contain the mapping from codes to text. The icd9 install and icd9p install then moves each of the datasets from the current directory to the directory in which the commands are installed.

## Syntax

Note: icd9 is for use with ICD-9 *diagnostic* codes and icd9p is for use with *procedure codes*. These are two commands whose syntax exactly parallels each other. Below we write icd9[p] to mean both commands:

```
icd9[p] check varname [, any list generate(newvar) ]
    icd9[p] clean varname [, <u>d</u>ots pad ]
    icd9[p] generate newvar = varname, main
    icd9[p] generate newvar = varname, description [long end]
    icd9[p] generate newvar = varname, range(icd9rangelist)
    icd9[p] lookup icd9rangelist
    icd9[p] \underline{sea}rch ["]text["] [["]text["] [...]] [, or]
    icd9[p] install [, replace]
    icd9p query
icd9rangelist is
                           icd9code
                                                meaning the particular code
                           icd9code*
                                                meaning all codes starting with icd9code
                           icd9code/icd9code
                                                meaning the code range including endpoints
```

or any combination of the above, such as "001\* 018/019 E\* 018.02". Note that *icd9codes* must be typed with leading zeros: 1 is an error; type 001 (diagnostic code) or 01 (procedure code).

## Description

icd9 and icd9p assist with working with ICD-9-CM codes. ICD-9-CM refers to the fifth edition of the International Classification of Diseases, 9th revision, Clinical Modification.

ICD-9 codes come in two forms: diagnostic codes and procedure codes. 001 (cholera), 572.0 (abscess of liver), 941.45 (deep 3rd deg burn nose), and E873 (watercraft explosion) are examples of diagnostic codes, although some people write (and datasets record) 94145 rather than 941.45. icd9 understands both ways of recording the codes. 01 (incise-excis brain/skill), 01.5 (skill biopsy), 55 (operations on kidney), and 55.01 (nephrotomy) are examples of procedure codes, although some people write 5501 rather than 55.01. icd9p understands both ways of recording codes.

icd9 and icd9p exactly parallel each other, it is just that icd9 is for use with diagnostic codes and icd9p for use with procedure codes. Below we will write icd9[p] to mean both commands.

icd9[p] check verifies that already existing variable varname contains valid ICD-9 codes. If not, icd9[p] check provides a full report on the problems. Use of icd9[p] check is optional. icd9[p] check is useful for tracking down problems when any of the other icd9[p] commands tell you "variable does not contain ICD-9 codes". icd9[p] check is a little more thorough, too, in that it verifies that each of the recorded codes actually exists in the official list.

icd9[p] clean also verifies that already existing variable varname contains valid ICD-9 codes and, if it does, icd9[p] clean modifies the variable to contain the codes in either of two standard formats—with or without the periods separating the main code from the detail. Use of icd9[p] clean is optional; all icd9[p] commands work equally well with cleaned or uncleaned codes. There are numerous ways of writing the same ICD-9 code and icd9[p] clean is designed (1) to ensure consistency and (2) to make subsequent output look better.

icd9[p] generate produces new variables based on already existing variables containing (cleaned or uncleaned) ICD-9 codes. icd9[p] generate, main produces *newvar* containing the main code. icd9[p] generate, description produces *newvar* containing a textual description of the ICD-9 code. icd9[p] generate, range() produces numeric *newvar* containing 1 if *varname* records an ICD-9 code in the range listed and 0 otherwise.

icd9[p] lookup and icd9[p] search are utility routines useful interactively. icd9[p] lookup simply displays descriptions of codes specified on the command line, so if you have a yearning to know what diagnostic E913.1 means, you can type "icd9 lookup e913.1". Whatever data you have in memory is irrelevant—and remains unchanged—when using icd9[p] lookup. icd9[p] search is like icd9[p] lookup except that it turns the problem around; icd9[p] search looks for relevant ICD-9 codes from the description given on the command line. For instance, you could type "icd9 search liver" or "icd9p search liver" to obtain a list of codes containing the word liver.

icd9[p] install has to do with installation of the icd9[p] command. See the section Completing the installation above.

icd9[p] query displays the identity of the source from which were obtained the ICD-9 codes and textual descriptions that icd9[p] uses.

Note that ICD-9 codes are commonly written two ways, with and without periods. For instance, with diagnostic codes, one can write 001, 86221, E8008, and V822, or one can write 001., 862.21, E800.8, and V82.2. With procedure codes, one can write 01, 50, 502, 5021, or one can write 01., 50., 50.2, 50.21. The icd9[p] command does not care which syntax you use or even whether you are consistent. Case also is irrelevant: v822, v82.2, v822, and v82.2 are all equivalent. Codes may be recorded with or without leading and trailing blanks.

## Options for use with icd9[p] check

- any tells icd9[p] check to verify the codes fit the format of ICD-9 codes but to skip checking whether the codes are actually valid. This makes icd9[p] check run faster. For instance, diagnostic code 230.52 (or 23052 if you prefer) looks to be valid, but in fact there is no such ICD-9 code, at least currently. Without the any option, 230.52 (23052) would be flagged as an error. With any, 230.52 (23052) is not considered an error.
- list tells icd9[p] check that invalid codes found in the data—1, 1.1.1, and perhaps 230.52 assuming any is not also specified—are to be individually listed.
- generate(newvar) specifies that icd9[p] check is to create new variable newvar containing, for each observation, 0 if the code is valid and a number from 1 to 10 if not. The positive numbers indicate the kind of problem and correspond to the listing produced by icd9[p] check. For instance, 10 means the code could be valid, it just turns out not to be on the official list.

## Options for use with icd9[p] clean

- dots specifies whether periods are to be included in the final format. Do you wish diagnostic codes recorded, for instance, 86221 or 862.21? Without the dots option, the former format is used. With the dots option, the latter format is used.
- pad specifies that the codes are to be padded with spaces, front and back, to make the codes line up vertically in listings. Specifying pad makes the resulting codes look better when used with most other Stata commands.

Technical Note: If you specify pad, the following character positions are used with *diagnostic* codes:

position	nodot	position	dot
1	E or " "	1	E or " "
2-4	rest of main code	2-4	rest of main code
5-6	detail code or spaces	5	"." or " "
		6–7	detail code or spaces

position	nodot
1–3 or 1–4 4–5 or 5–6	optional $E$ + rest of main code detail code or nothing
nosition	det
position	dot
position 1–3 or 1–4	dot optional E + rest of main code
position 1–3 or 1–4 4 or 5	dot optional E + rest of main code "." or nothing

If pad is not specified, the ICD-9 diagnostic code is written without leading or trailing blanks, meaning

With procedure codes (which never have leading letters), the column positions when pad is specified are

position	nodot	position	dot
1–2 3–4 5	main code detail code or spaces	1-2 3 4-5	main code "." or " " detail code or spaces

If pad is not specified, the ICD-9 procedure code is written without trailing blanks.

## Options for use with icd9[p] generate

main, description, and range() specify what icd9[p] generate is to calculate. In all cases, *varname* specifies a variable containing ICD-9 codes.

main specifies that the main code is to be extracted from the ICD-9 code. For procedure codes, the main code is the first two characters. For diagnostic codes, the main code is usually the first three or four characters (the characters before the dot if the code has dots). In any case, icd9[p] generate does not care whether the code is padded with blanks in front or how strangely it might be written; icd9[p] generate will find the main code and extract it. The resulting variable is itself an ICD-9 code and may be used with the other icd9[p] subcommands. This includes icd9[p] generate, main because main codes of main codes are main codes.

description creates newvar containing descriptions of the ICD-9 codes.

long is for use with description. It specifies that the new variable, in addition to containing the text describing the code, is to contain the code, too. Without long, *newvar* in an observation might contain "bronchus injury-closed". With long, it would contain "862.21 bronchus injury-closed".

end modifies long and places the code at the end of the string: "bronchus injury-closed 862.21". Specifying end implies long.

range() allows you to create indicator variables equal to 1 when the ICD-9 code is in the inclusive range specified.

#### Options for use with icd9[p] search

or specifies that ICD-9 codes are to be searched for any entry that contains any of the words specified after icd9[p] search. The default is to list only entries that contain all the words specified.

## Options for use with icd9[p] install

replace specifies that the completion of the installation is to be done again. Specify replace if you type icd9[p] install, are told that you have already done that, and really do want to reinstall.

#### Remarks

Let us begin with diagnostic codes-the codes icd9 processes. The format of an ICD-9 diagnostic code is

blanks  $\{0-9, V, v\}$   $\{0-9\}$   $\{0-9\}$  [.] [0-9[0-9]] blanks

or

 $\left[blanks\right]\left\{E,e\right\}\left\{0-9\right\}\left\{0-9\right\}\left\{0-9\right\}\left[.\right]\left[0-9\left[0-9\right]\right]\left[blanks\right]$ 

i cd9 can deal with ICD-9 diagnostic codes written any of the ways the above allows. Items in square brackets are optional. The code might start with some number of blanks. Braces  $\{ \}$  indicate required items. The code either then has a digit from 0 to 9

and

or the letter V (uppercase or lowercase) (first line) or it has the letter E (uppercase or lowercase, second line). After that, it has two or more digits, perhaps followed by a period, and after that it may have up to two more digits (perhaps followed by more blanks).

All of the following meet the above definition:

001 001. 001.9 0019 86222 862.22 E800.2 e8002 V82 V82 V822 V822

Meeting the above definition does not make the code valid. There are 233,100 possible codes meeting the above definition, of which 15,186 are currently defined.

Examples of currently defined diagnostic codes include

code	description
001	cholera*
001.0	cholera d/t vib cholerae
001.1	cholera d/t vib el tor
001.9	cholera nos
999	complic medical care nec*
V01	communicable dis contact*
V01.0	cholera contact
V01.1	tuberculosis contact
V01.2	poliomyelitis contact
V01.3	smallpox contact
V01.4	rubella contact
V01.5	rabies contact
V01.6	venereal dis contact
V01.7	viral dis contact nec
V01.8	communic dis contact nec
V01.9	communic dis contact nos
 F800	rr collision nos*
E800 0	rr collision nos-employ
E800 1	rr coll nos-passenger
E800 2	rr coll nos-pedestrian
E800.3	rr coll nos-ped cyclist
E800.8	rr coll nos-person nec
E800.9	rr coll nos-person nos
	-

"Main codes" refer to the part of the code to the left of the period. 001, 002, ..., 999, V01, ..., V82, E800, ..., E999 are main codes. There are 1,182 diagnostic main codes.

The main code corresponding to a detailed code can be obtained by taking the part of the code to the left of the period, except for codes beginning with 176, 764, 765, v29, and v69. Those main codes are not defined and yet, there are more detailed codes under them:

(Continued on next page)

code	description
176	CODE DOES NOT EXIST, but 8 codes starting with 176 do exist:
176.0	skin - kaposi's sarcoma
176.1	sft tisue - kpsi's srcma
764	CODE DOES NOT EXIST, but 44 codes starting with 764 do exist:
764.0	lt-for-dates w/o fet mal*
764.00	light-for-dates wtnos
765 765.0 765.00	CODE DOES NOT EXIST, but 22 codes starting with 765 do exist: extreme immaturity* extreme immatur wtnos
V29	CODES DOES NOT EXIST, but 6 codes stating with V29 do exist:
V29.0	nb obsrv suspct infect
V29.1	nb obsrv suspct neurlgcl
V69	CODE DOES NOT EXIST, but 6 codes starting with V69 do exist:
V69.0	lack of physical exercse
V69.1	inapprt diet eat habits

Our solution is to define four new codes:

code	description
176	kaposi's sarcoma (Stata)*
764	light-for-dates (Stata)*
765	immat & preterm (Stata)*
V29	nb suspct cnd (Stata)*
V69	lifestyle (Stata)*

Thus, there are 15,186 + 5 = 15,191 diagnostic codes of which 1,181 + 5 = 1,186 are main codes.

Things are less confusing with respect to procedure codes—the codes processed by icd9p. The format of ICD-9 procedure codes is

 $\left[blanks\right]\left\{0-9\right\}\left\{0-9\right\}\left[.\right]\left[0-9\left[0-9\right]\right]\left[blanks\right]$ 

Thus, there are 10,000 possible procedure codes of which 4,275 are currently valid. The first two digits represent the main code, of which there are 100 feasible and 98 are currently used (00 and 17 are not used).

## Descriptions

The descriptions given for each of the codes is as found in the original source with, in the case of procedure codes, the addition of five new codes by us. An asterisk on the end of a description indicates that the corresponding ICD-9 diagnostic code has subcategories.

icd9[p] query reports the original source of the information on the codes:

```
. icd9 query
_dta:
 1. Dataset obtained 24aug1999
  2. from http://www.hcfa.gov/stats/pufiles.htm
  3. file http://www.hcfa.gov/stats/icd9v16.exe
  4. Codes 176, 764, 765, V29, and V69 defined
  5. -- 176 kaposi's sarcoma (Stata)*
  6. -- 765 immat & preterm (Stata)*
 7. -- 764 light-for-dates (Stata)*
  8. -- V29 nb suspct cnd (Stata)*
  9. -- V69 lifestyle (Stata)*
. icd9p query
_dta:
 1. Dataset obtained 24aug1999
  2. from http://www.hcfa.gov/stats/pufiles.htm
  3. file http://www.hcfa.gov/stats/icd9v16.exe
```

## Example

You have a dataset containing up to three diagnostic codes and up to two procedures on a sample of 1,000 patients:

. use	patients	, clear				
. list	in 1/10					
	patid	diag1	diag2	diag3	proc1	proc2
1.	- 1	65450			9383	
2.	2	23v.6	37456		8383	17
з.	3	V10.02				
4.	4	102.6			629	
5.	5	861.01				
6.	6	38601	2969		9337	
7.	7	705			7309	8385
8.	8	v53.32			7878	951
9.	9	20200	7548	E8247	0479	
10.	10	464.11	20197		4641	

Do not try to make sense of this data because, in constructing this example, the diagnostic and procedure codes were chosen at random.

Begin by noting that variable diag1 is recorded sloppily—sometimes the dot notation is used, sometimes not, and sometimes there are leading blanks. That does not matter. We decide to begin by using icd9 clean to clean up this variable:

. icd9 clean diag1 diag1 contains invalid ICD-9 codes r(459);

icd9 clean refused because there are invalid codes among the 1,000 observations. We can use icd9 check to find out about the problems:

. icd9 (	check diag1	
diag1 c	ontains invalid codes:	
1.	Invalid placement of period	0
2.	Too many periods	0
з.	Code too short	0
4.	Code too long	0
5.	Invalid 1st char (not 0-9, E, or V)	0
6.	Invalid 2nd char (not 0-9)	0
7.	Invalid 3rd char (not 0-9)	1
8.	Invalid 4th char (not 0-9)	0
9.	Invalid 5th char (not 0-9)	0
10.	Code not defined	0
	Total	1

There is only one observation with a problem. We can find that observation by asking icd9 check to flag the problem observations (or observation, as it is in this case):

. icd9 check diag1, gen(prob)	
diag1 contains invalid codes:	
1. Invalid placement of period	0
2. Too many periods	0
3. Code too short	0
4. Code too long	0
5. Invalid 1st char (not 0-9, E, or V)	0
6. Invalid 2nd char (not 0-9)	0
7. Invalid 3rd char (not 0-9)	1
8. Invalid 4th char (not 0-9)	0
9. Invalid 5th char (not 0-9)	0
10. Code not defined	0
Total	1
list natid diag1 prob if prob	-
. Hist patid diagi prob II prob	
patid diagi prob	
2. $2 23 v. 6$ 7	

Let's assume we go back to the patient records and determine that this should have been coded 230.6:

. replace diag1 = "230.6" if patid==2
(1 real change made)
. drop prob

We now try again to clean up the formatting of the variable:

. icd9 clean diag1
(643 changes made)
. list in 1/10

	patid	diag1	diag2	diag3	proc1	proc2
1.	1	65450			9383	
2.	2	2306	37456		8383	17
з.	3	V1002				
4.	4	1026			629	
5.	5	86101				
6.	6	38601	2969		9337	
7.	7	705			7309	8385
8.	8	V5332			7878	951
9.	9	20200	7548	E8247	0479	
10.	10	46411	20197		4641	

Perhaps we prefer the dot notation. icd9 clean can be used again on diag1, and now we will continue to clean up diag2 and diag3:

. icd9 (936 ch	clean d anges m	iag1, dots ade)				
. icd9 (551 ch	clean d anges m	iag2, dots ade)				
. icd9 (100 ch	clean d anges m	iag3, dots ade)				
. list	in 1/10					
	patid	diag1	diag2	diag3	proc1	proc2
1.	1	654.50			9383	
2.	2	230.6	374.56		8383	17
з.	3	V10.02				
4.	4	102.6			629	
5.	5	861.01				
6.	6	386.01	296.9		9337	
7.	7	705			7309	8385
8.	8	V53.32			7878	951
9.	9	202.00	754.8	E824.7	0479	
10.	10	464.11	201.97		4641	

We now turn to cleaning the procedure codes. We use icd9p (emphasis on the p) to clean these codes:

icd9] (816 cl	p clean hanges m	proc1, do ade)	ts			
icd9] (140 cl	p clean hanges m	proc2, do ade)	ts			
list	in 1/10					
	patid	diag1	diag2	diag3	proc1	proc2
1.	1	654.50	-	-	93.83	-
2.	2	230.6	374.56		83.83	17
3.	3	V10.02				
4.	4	102.6			62.9	
5.	5	861.01				
6.	6	386.01	296.9		93.37	
7.	7	705			73.09	83.85
8.	8	V53.32			78.78	95.1
9.	9	202.00	754.8	E824.7	04.79	
10.	10	464.11	201.97		46.41	

It is important to understand that both icd9 clean and icd9p clean only verify that the variable being cleaned follows the construction rules for the code; it does not check that the code is itself valid. icd9[p] check does that:

. icd9p check proc1 (proc1 contains valid ICD-9 procedure codes; 168 missing values) . icd9p check proc2 proc2 contains invalid codes: 1. Invalid placement of period 0 Too many periods
 Code too short 0 0 4. Code too long 0 5. Invalid 1st char (not 0-9) 0 6. Invalid 2nd char (not 0-9) 0 7. Invalid 3rd char (not 0-9) 0 8. Invalid 4th char (not 0-9) 0 10. Code not defined 1 Total 1

Note that diag2 has an invalid code. We could find it using icd9p check, generate() just as we previously found the bad diagnostic code using icd9 check, generate().

icd9[p] can create new variables containing textual descriptions of our diagnostic and procedure codes. For instance,

. i	cd9	gen to	l1 = d	liag1,	lesc	
. so	ort	patid				
. 1:	ist	patid	diag1	td1	n 1/10	
		patio	d dia	ig1	td1	
1		1	654	.50	cerv in	ncompet preg-unsp
2		2	2 2 3 0	).6	ca in s	situ anus nos
3		3	3 V1C	0.02	hx-oral	l/pharynx malg nec
4		4	102	2.6	yaws of	f bone & joint
5		5	5 861	.01	heart o	contusion-closed
6		e	386	5.01	meniere	e dis cochlvestib
7		7	705	i	disorde	ers of sweat gland*
8		8	3 V53	3.32	ftng au	utmtc dfibrillator
9		9	9 202	2.00	ndlr ly	ym unsp xtrndl org
10		10	) 464	.11	ac tra	cheitis w obstruct

Note that icd9[p] generate, description does not preserve the sort order of the data (and neither does icd9[p] check unless you specify the any option).

Recall that procedure-code proc2 had an invalid code. Even so, icd9p generate, description is willing to create a textual description variable:

```
. icd9p gen tp2 = proc2, desc
(1 non-missing values invalid and so could not be labeled)
. sort patid
. list patid proc2 tp2 in 1/10
       patid proc2
                         tp2
 1.
           1
 2.
           2 17
 з.
           3
 4.
           4
 5.
           5
 6.
           6
 7.
           7
              83.85
                         musc/tend lng change nec
 8.
           8 95.1
                         form & structur eye exam*
 9.
           9
10.
           10
```

tp2 contains nothing when proc2 is 17 because 17 is not a valid procedure code.

icd9[p] generate can also create variables containing main codes:

```
. icd9 gen main1 = diag1, main
. list patid diag1 main1 in 1/10
       patid diag1
                             main1
 1.
           1 654.50
                               654
 2.
           2 230.6
                               230
 з.
           3 V10.02
                               V10
 4.
           4 102.6
                               102
 5.
           5
              861.01
                               861
 6.
           6 386.01
                               386
 7.
           7
              705
                               705
 8.
           8
              V53.32
                               V53
 9.
                               202
           9 202.00
10.
          10 464.11
                               464
```

icd9p generate, main can similarly generate main procedure codes.

Sometimes one is merely examining an observation:

. list diag\* if patid==563 diag1 diag2 diag3 563. 526.4

If we wondered what 526.4 was, we could type

icd9[p] lookup has the ability to list ranges of codes:

```
. icd9 lookup 526/527
12 matches found:
    526
             jaw diseases*
    526.0
             devel odontogenic cysts
    526.1
             fissural cysts of jaw
    526.2
             cysts of jaws nec
    526.3
             cent giant cell granulom
    526.4
             inflammation of jaw
    526.5
             alveolitis of jaw
    526.8
             other jaw diseases*
    526.81
             exostosis of jaw
    526.89
             jaw disease nec
    526.9
             jaw disease nos
    527
             salivary gland diseases*
```

icd9[p] search has the ability to go from description to code:

```
. icd9 search jaw disease
4 matches found:
    526    jaw diseases*
    526.8    other jaw diseases*
    526.89    jaw disease nec
    526.9    jaw disease nos
```

## Saved results

icd9[p] check saves scalars r(e1), r(e2), ..., r(e10) reporting the number of errors of type 1, 2, ..., 10, and r(esum) reporting the total number of errors.

dm77	Removing duplicate observations in a dataset
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Abstract: A command is given that removes duplicated observations in a dataset and retains the unique observations without repetition.

Keywords: Duplicated observations.

#### Syntax

unique1 using filename

## Description

unique 1 removes the duplicated observations in the current dataset and retains the unique observations without any repetition. The observations are in the same order as the original dataset except that repeated observations are deleted. If *filename* is specified without an extension, .dta is assumed.

## Remarks

The disk dataset must be a Stata-format dataset; that is, it must have been created using the save command.

#### Examples

You have a dataset stored on disk that you wish to remove the duplicated observations.

	use tes	tdata		
•	list			
		id	x	у
	1.	2	01/08/76	Α
	2.	2	01/08/76	Α
	3.	3	14/04/98	A
	4.	3	14/04/98	В
	5.	3	14/04/98	В
	6.	1	22/01/64	С
	7.	1	22/01/64	С
	8.	1	14/10/87	С
	clear			

unique1	using	testdata	
list			
	id	х	У
1.	2	01/08/76	A
2.	3	14/04/98	A
3.	3	14/04/98	В
4.	1	22/01/64	C
5.	1	14/10/87	C

gr34.3	An update to drawing Venn diagrams

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Abstract: When John Venn (1834-1923) published his work on logic and developed the "Venn Diagram", he used circles to indicate the combination of two and three variables and ellipses to show the combination of four variables. The previous version of the venndiag routine used squares to represent the combinations. The current update extends the design of the Venn Diagram to use circles or ellipses. Venn diagrams are useful when one wishes to either show overlapping combinations of simultaneous outcomes e.g., displaying which of the allergens birch tree, cat, molds, and so on, make you wheeze on a graph, or when the user wishes to calculate a new variable which reflects those combinations.

Keywords: Venn Diagram, ellipse, multiple-choice answers.

## Introduction

When John Venn (1834–1923) published his work on logic and developed the "Venn Diagram", he used circles to indicate the combination of two and three variables and ellipses to show the combination of four variables. The previous versions of the venndiag routine introduced in Lauritsen (1999a, 1999b, 1999c) used squares to represent the combinations. The current update extends the design of the Venn Diagram to use circles or ellipses. The user can specify the desired design as an option.

The syntax has been slightly changed with addition of the design types with options square, ellipse, and circle and two placement options xoff and yoff which set distances of titles from the top of the diagram and the left margin, respectively. A few adaptations as a consequence of the changed design have been made to other options, as described in the help file for venndiag.

#### New syntax

venndiag varlist [if exp] [in range] [, square ellipse circle label(str) show(str) missing
gen(varnames) list(variables) print saving(filename) c1(#) c2(#) c3(#) c4(#) noframe
nograph nolabel t1title(str) t2title(str) t3title(str) r1title(str) r2title(str) r3title(str)
r4title(str) r5title(str) r6title(str) pen(#) thick(#) xoff(#) yoff(#) ca(#) ]

The varlist must contain from two to four numerical variables and if generating a variable, that variable must be nonexisting.

## New options

square shows rectangles as in previous versions.

ellipse shows ellipses with two to four variables (this is the default for four variables).

circle shows circles (this is the default for two or three variables).

- xoff(#) defines the top margin, that is, the distance from the top to r1title with a default value of 6000 in Stata's graphics coordinates.
- yoff(#) defines the left margin, that is, the distance from the left to r1title with a default value of 22000 in Stata's graphics coordinates.
- ca(#) tells venndiag to count on specified value for all variables, e.g., ca(2) means to use 2 as the outcome.

#### Examples

Using examples similar to those in Lauritsen (1999a), we show that the default design for two and three variables is circles as shown in Figures 1 and 2.

. venndiag astma season



Figure 1. A simple example of two variables.

. venndiag astma season eczema, saving(figure2)



Figure 2. A simple example of three variables.

For four variables, the default is ellipses as shown in Figure 3. Variable labels and percentages are placed in relation to the circle or ellipse which represents each variable. Some experimentation might be needed if you have long labels.

. venndiag eczema astma season atopia, ellipse



Figure 3. Ellipses used for displaying four variables.

## **Drawing ellipses**

When drawing the ellipses, a procedure similar to the following is used. The program lines for drawing ellipses are actually quite simple. The idea is to first save your own data as a temporary file (before), clear, and generate 1000 (x, y) points based

on the formula for an ellipse, draw a graph of this and then finally restore your own data. Try experimenting with the last parameters, which define the shape of the ellipses.

```
program define ellipse
                                /* draw ellipse on screen */
version 6
  /* parameters 1: Rotation of ellipse in degrees 2:offset X 3:offset Y 4+5: defines shape of ellipse* /
  tempfile before
  save `before'
  local V = (`1'/360)* 2*_pi
  local lam = `4'
                           /*size of ellipse ~ length */
  local eps = `5'
                          /*shape of ellipse ~ if = 0 the result will be a circle*/
  local offx = 2^{\prime}
  local offy = `3'
  clear
  set obs 1001
  tempvar i x y
  gen `i' = -_pi+(2*_pi/1000)*(_n-1)
  gen `x' = ((1+`eps')*(`lam')*cos(`i'))/(1+(`eps')*cos(`V'-`i'))*100 + `offx'
  gen `y´ = ((1+`eps´)*(`lam´)*sin(`i´))/(1+(`eps´)*cos(`V´-`i´))*100 + `offy´
  gph open
  gph vline `y´ `x´
  gph text 2000 18000 0 -1 Angle in this graph is `1'
gph text 3500 18000 0 -1 Offset X: `2' Offset Y: `3'
  gph text 4500 18000 0 -1 Parameter: Size=`4' Shape=`5'
  gph close
  use `before', clear
end
ellipse 90 15000 20000 15 0.854
more
ellipse 180 5000 6000 8 0.9
more
ellipse 180 5000 8000 25 0.65
```

#### Acknowledgments

Martin Villumsen sorted out the mathematics of drawing ellipses in different angles. Thanks to N. Cox who provided the idea for adding circles to a graph and to Alan Riley at Stata Corporation for help on macros and passing values to programs.

#### References

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gr43	Overlaying graphs
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**Abstract:** This function allows multiple graphs to be displayed on common axes. As any graphical function is allowed, this command can produce graphs for longitudinal data or looking at overlayed histograms.

Keywords: Graphs, stratified graphs.

#### Syntax

```
overlay varlist [if exp], by(varlist) [saving(filename) function(str) ylab(numlist) xlab(numlist)
```

```
graph_options
```

## Options

by(varlist) specifies the strata for the multiple graphs.

saving(filename) saves the graph as filename.gph.

function(str) specifies the command that draws the graph. If this is not specified, then the graph function is used.

ylab(numlist) specifies axes labels.

xlab(numlist) specifies axes labels.

## Description

This function draws several graphs in one area of the graphics window. As a result this function is very versatile and will work well with any graph function that allows the user to specify the axes. The function will, by default, try to calculate axes that remain unchanged for each graph, this may fail and the user then has to specify the axes using xlab and ylab.

Any options for the graphing function can be added to the end of the command line. These can be options such as the plotting symbol and connecting points.

## Examples

Data is taken from a clinical trial that measures peak flow for asthma sufferers over time. To plot individual lines per person through time is achieved by

. overlay pef day0, by(patient) c(l) s(.) sort saving(graph1)

which produces the graph in Figure 1.



Figure 1. Plotting lines for several people in a clinical trial.

The varlist is passed directly to graph so pef is on the y-axis.

To illustrate the use of kdensity instead of graph, consider

```
. overlay pef if patient<5028, by(patient) function(kdensity) xlab(150,350,680) ylab(0,0.02, 0.045) s(.)
```

For kdensity it was necessary to specify the axes since otherwise the graph would be incorrect. Figure 2 shows the kernel density estimates for 4 patients.



Figure 2. Kernel density estimates for four people.

Note that overlay can even overlay histograms although this may seem a little confusing in black and white. Consider Figure 3 which results from

. overlay pef if patient<5028, by(patient) xlab(150,350,680) bin(8) ylab(0,1.1)



Figure 3. Overlaying histograms.

|--|

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Abstract: The archutil package published in STB-52 for working with files or packages in the Statistical Software Components archive has been extensively revised. archlist has been superseded by archdesc, which offers additional features and incorporates a correction regarding behavior when logging. A new component, archinst, allows the user to install a package from the archive in one command.

Keywords: SSC-IDEAS, Statalist, internet, files, packages, archutil.

The archutil package published by Baum and Cox (1999) has been extensively revised. The original version contained utilities archlist, archtype and archcopy. archlist has been superseded by archdesc, which offers additional features and incorporates a correction regarding behavior when logging. A new component, archinst, allows the user to install a package from the archive in one command.

These commands work with files or packages from the Statistical Software Components (SSC) archive (often called the Boston College archive). They require a net-aware variant of Stata 6.0.

## Syntax

```
archdesc [ { package | letter } ][ using filename ][, replace nolog ]
archinst package [, net_install_options ]
archcopy filename.ext [, copy_options ]
archtype filename.ext
```

## Description

archdesc describes the contents of the archive.

archdesc, with neither a letter nor a package specified, lists all packages in the archive. By default, it also puts a log of the listing in ssc-ideas.lst.

archdesc letter (where letter is one of a-z or \_) lists all packages in the archive whose names begin with that letter.

archdesc *package* (where *package* is a name two or more letters long beginning with a-z or \_) describes that package if it exists; or all packages beginning with the same letter if it does not. Thus a faulty guess still produces information on nearby names.

If archdesc is accompanied by logging results to a file, any existing logging is temporarily suspended.

archinst *package* installs that package from the archive.

archcopy *filename.ext* copies *filename.ext* from the SSC archive to the appropriate directory or folder within STBPLUS, determined automatically. (If curious, type sysdir to see where this is.) This is appropriate for individual .ado or .hlp files. archcopy is rarely needed, given archinst.

archtype filename.ext types filename.ext from the SSC archive. This is appropriate for individual .ado or .hlp files.

## Options

replace specifies that *filename* is to be overwritten.

nolog overrides the default behavior of archdesc, with no specification of either a letter or a package, which is to log to ssc-ideas.lst.

net\_install\_options are options of net install. See help on net or [R] net.

copy\_options are options of copy. See help on copy or [R] copy.

## archdesc and logging

Depending on how it is called, archdesc varies in whether it echoes results to a log file by default.

archdesc by itself will produce quite lengthy output (as of January 2000, more than 600 lines). Such output may be too much to scan visually with ease, and it has some value as a reference source. The default is therefore that output will be echoed to a log file. This default can be overridden with the nolog option.

In contrast, archdesc with a letter or package name produces much less output, which will not be logged to a file unless explicitly requested.

Logging here refers to opening a log file for archdesc results and closing it afterwards, which are all handled automatically by archdesc. Any existing logging is temporarily suspended.

However, if you are already logging to a file, and wish the results of archdesc to be included in the log with other results of your session, then that is achieved by issuing either archdesc, nolog or archdesc *whatever* within your session. The earlier opening and (if desired) later closing of the log are the user's responsibility, as usual.

#### archdesc and archlist

archdesc supersedes archlist, documented by Baum and Cox (1999).

archlist as published by Baum and Cox (1999) would not resume logging to a log file previously being used if there was a problem with the using subcommand. Suppose, for example, that a user had typed

- . log using log1
- . archlist using log2

and log2.log already existed. The correct syntax would have been

```
. archlist using log2, replace
```

The syntax error would have halted the program, but logging to log1.log would not have been resumed.

archdesc handles this problem more gracefully. In addition, a corrected version of archlist is included on the electronic media (floppy disk or website copies) accompanying this insert, even though users are recommended to switch to archdesc.

#### Examples

In the examples below the somewhat lengthy output of these commands is suppressed here to save space.

```
archdesc using ssc.txt, replace
archdesc w
archdesc whitetst using whitetst.txt
archcopy whitetst.ado
archcopy whitetst.hlp
archtype whitetst.hlp
```

## Acknowledgments

Helpful advice was received from Bill Gould, Jens Lauritsen, Vince Wiggins, and Desmond Williams.

## Reference

Baum, C. F. and N. J. Cox. 1999. ip29: Metadata for user-written contributions to the Stata programming language. Stata Technical Bulletin 52: 10-12.

sbe32	Automated outbreak detection from public health surveillance data
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Abstract: The early detection of outbreaks in epidemiological surveillance is an important challenge in order to introduce effective control measures. In this insert, we adapt and program an algorithm developed by Farrington et al. (1996) to process weekly reports of infectious diseases, which is based on a loglinear regression model. The output is a threshold value for the current week above which the observed count is declared to be unusual.

Keywords: Outbreak, regression, threshold, public health surveillance.

#### Introduction

Epidemiological surveillance is the systematic collection, analysis, and interpretation of data for public health purposes. One of its aims is the early detection of outbreaks in order to introduce effective control measures. Many available methods for this purpose are based on parametric procedures, which compare actual numbers of cases with a warning threshold calculated from historical data. The statistical methodology to do the detection of unusual disease clusters must cope with several difficulties as fluctuations in the historical data series may be due to seasonal cycles and secular trends, and by past outbreaks. In addition, the method must be sufficiently robust to accommodate a wide range of microorganisms. The available methodology is reviewed in Farrington et al. (1996). In this paper, the authors developed an automated procedure to process weekly reports of infectious diseases, which is based on a loglinear regression model, adjusted for overdispersion, seasonality, secular trends, and past outbreaks. The model is used to calculate an expected value for the current week based on historical data, together with a threshold value above which an observed count is declared to be unusual. The baseline data to fit the regression model are specified by the following mechanism: if the current week is  $t_0$ , only data from weeks  $t_0 - 3$  to  $t_0 + 3$  from the previous five years are included. In this insert, we present a program to calculate threshold values using a modified version of Farrington's algorithm. The data are weekly reports of infectious disease from a passive surveillance system based on laboratory reporting.

#### Methodology

The baseline count  $y_i$  is assumed to be generated by a Poisson-like process, except that the variation is greater than that of a true Poisson for some organisms. In this case, negative binomial regression is used to estimate the model for the weekly counts from historical data. We assume a serial correlation between baseline counts within the same year and independence otherwise. The model fitted is

$$\begin{split} y_i \sim \text{Poisson}(g_i) \\ g_i = \exp(\alpha + \beta t_i + \delta n_i + u_i) = \exp(\alpha + \beta t_i + \delta n_i) \exp(u_i) = m_i e_i \end{split}$$

where  $e_i$  is the random effect of the model, and  $\mu_i$  is the systematic component. The random effect  $e_i$  is assumed to follow a gamma distribution with mean one and variance  $(\phi - 1)/\mu_i$ ,  $\phi$  being the overdispersion parameter:

$$e_i \sim \text{Gamma}\left(\frac{\mu_i}{\phi - 1}, \frac{\mu_i}{\phi - 1}\right)$$

resulting in the negative binomial distribution with mean  $\mu_i$  and variance  $\phi \mu_i$  for the baseline count  $y_i$ . The Poisson model corresponds to  $\phi = 0$ , while  $\mu_i$ , the systematic component, can be modeled as

$$\log \mu_i = \alpha + \beta t_i + \delta n_i$$

where  $\beta t_i$  is a linear time trend that is omitted if not significant, and  $\delta n_i$  adjusts the geographic effect in reporting. This is an additional component to the model used in Farrington's algorithm. Moreover, we have introduced several modifications related to the estimation procedure. The variables included in the model are  $y_i$ , the number of cases reported at week i,  $t_i$ , the time measured in weeks, and  $n_i$ , the number of hospitals reporting cases at week i.

The model yields a 99% prediction interval for the current week, and the threshold value is calculated as the upper limit of that interval. When no cases are reported in a week, we assume that no outbreak occurred and thus no model is fitted. As a consequence, no threshold is calculated.

The output of the program is a table displaying the list of microorganisms with the observed number of cases and the threshold value for the current week. In addition, a warning message is displayed when the actual report exceeds the threshold.

#### Syntax

obvset [ var1 var2 var3 var4 var5 ] outbrk #week #year

- where *var1* is the numerical variable of reports, *var2* is the numerical variable identifying the week, *var3* is the numerical variable identifying the year, *var4* is the numerical variable with the number of hospitals reporting the cases, and *var5* is the string variable containing the name of the microorganisms.
- The arguments  $\#_{week}$  and  $\#_{year}$  are, respectively, the number of the weeks and years in which we want to detect if an outbreak has occurred. outbrk works after setting the variables with obvset.

## Description

outbrk calculates threshold values for outbreak detection of infectious diseases based on historical data. It was developed for data consisting of weekly reports of positive microbiological diagnostics from a passive surveillance system based on laboratory reporting.

outbrk can be used for outbreak detection within other surveillance systems of communicable diseases weekly reporting.

obvset doesn't allow the user to save these settings with the dataset. When exiting Stata, the current settings are cleared. obvset will be helpful if you need to run outbrk for different weeks. Without arguments, obvset displays current settings, if any.

Note that outbrk uses poisml introduced in Hilbe (1998).

## Example

We illustrate the use of outbrk with salmonella data from the National Microbiological Reporting System (SIM). The data consist of weekly reports of serotyping salmonella species, one of the most common reported cause of gastrointestinal infection, from the above surveillance system within the period 1992–1998. In this example, we apply outbrk for the detection of the possibility of existence of outbreaks due to different salmonella serotypes in the third week of the year 1998. First, we describe the dataset:

```
. describe
Contains data from salmo.dta
 Microbiological weekly reports of salmonella
            3,360
 obs:
 vars:
               5
                              164,7
                  size:
  _____
              ____
                    _____
  1. organism str25
                   %25s
                                       microorganism name
  2. year
             float
                   %6.0g
                                       year identify number
  3. week
             float
                   %6.0g
                                       week identify number
                   %6.0g
  4. counts
             float
                                       number of cases reported
  5. nhosp
             float
                   %6.0g
                                       number of hospitals
                                       reporting
_____
```

Typing obvset without arguments, we verify that no variables have been set. Therefore, we have to set the variables by typing . obvset counts week year nhosp organism

Now, if we type obvset without arguments:

. obvset Reports count is:COUNTS Week identifier is:WEEK Year identifier is:YEAR Hospitals count is:NHOSP Organism identifier is:ORGANISM

After setting the variables, we can use outbrk:

•	out	brk	3	1998	
ΥE	AR	1998	3;	WEEK	3

·+-			
Organism	Reports	Threshold	Warning
S.enteritidis	17	34.76	-
S.infantis	0		-
S.typhimurium	19	18.29	Warning
S.virchow	0		-
Salmonella gr.B	6	17.20	-
Salmonella gr.C	0		-
Salmonella gr.C1	0		-
Salmonella gr.C2	1	3.01	-
Salmonella gr.D	2	6.91	-
Salmonella sp.	15	27.59	-
+			

This table shows the different salmonella serotypes list, the reports in the third week of 1998, the calculated threshold value, and a warning message if the reported counts exceed that value. In this week, the number of cases reported for Salmonella typhimurium exceeds the threshold value, so a further epidemiological investigation is needed to check if this warning is an outbreak. There are no counts reported for S. Infantis, S. Virchow, Salmonella gr. C and Salmonella gr. C1; therefore no threshold value was calculated. This detection system provides epidemiologists with a tool for use in conjunction with other surveillance methods. Its main function is to focus attention on a potential outbreak, which is especially valuable when large numbers of different microorganisms are reported each week.

#### Acknowledgments

This work was presented at the First Iberian Stata User's Group meeting, which was held the 20th and 21st of May in Cordoba, Spain. Thanks to Aurelio Tobias for helpful comments. The data in the example are from the National Microbiological Reporting System.

## References

- Farrington, C. P., N. J. Andrews, A. D. Beale, and M. A. Catchpole. 1996. A statistical algorithm for the early detection of outbreaks of infectious disease. Journal of the Royal Statistical Society, Series A 159: 547–563.
- Hilbe, J. 1998. sg91: Robust variance estimators for MLE Poisson and negative binomial regression. Stata Technical Bulletin 45: 26–28. Reprinted in Stata Technical Bulletin Reprints, vol. 8, pp. 177–180.

sg84.2	Concordance correlation coefficient: update for Stata 6
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Abstract: The program for concordance correlation previously published in STB-43 and STB-45 has been updated to the syntax of Stata 6.0 and corrected for some deficiencies, principally to do with graphics and speed of calculation. A new option now permits the saving of the standard normal plot.

Keywords: Concordance correlation, graphics, measurement comparison.

#### Description

concord computes Lin's (1989) concordance correlation coefficient,  $\rho_c$ , for agreement on a continuous measure obtained by two persons or methods and provides an optional graphical display of the observed concordance of the measures. concord also provides statistics and optional graphics for Bland and Altman's (1986, 1995) limits-of-agreement, *loa*, procedure. The *loa*, a data-scale assessment of the degree of agreement, is a complementary approach to the relationship-scale approach of  $\rho_c$ .

This insert documents enhancements and changes to concord and provides the syntax needed to use a new feature. A full description of the method and of the operation of the original command and options was given by Steichen and Cox (1998a). A few revisions were documented later by Steichen and Cox (1998b). This updated program does not change the implementation of the underlying statistical methodology, or modify the original operating characteristics of the program; rather, it follows the syntax changes of Stata version 6.0.

#### Syntax

```
concord varl var2 [weight] [if exp] [in range] [, by(byvar) summary level(#) graph({ccc | loa})
noref reg npsaving(filename [, replace]) nosnd(snd_var [, replace]) graph_options ]
```

#### New option

npsaving(filename [, replace]) saves the standard normal plot generated by graph(loa). The filename is assumed to have extension gph. If filename does not exist, it is created. If filename exists, an error will occur unless replace is also specified. This option is ignored if graph(loa) is not requested. Note that the usual saving() option saves the loa plot itself when graph(loa) is specified (and the concordance plot when graph(ccc) is specified).

## Explanation

The primary purpose of this version is to revise concord to meet and to exploit syntax changes in Stata 6. In addition, some deficiencies in the previous implementation have been corrected.

First, concord previously failed when attempting a saving() of the loa plot generated by the graph(loa) option. This has been fixed. Second, the program did not allow the standard normal plot, which is also generated by the graph(loa) option,

to be saved. The new npsaving() option now allows that. Third, it did not allow variable labels to appear on the axes of the loa graph in place of variable names. They will now appear if they are defined. Fourth, a few minor changes have been made to speed up calculation.

A consequence of updating to Stata 6 is that the workarounds t1title(".") and t2title(".") to blank out default titles are no longer required. Blanking out can now be obtained directly by, for example, t1title("") and the previous workarounds now work literally, placing a period in the requested title.

## Saved Results

The system  $S_{\#}$  macros are unchanged. In addition, the saved results are returned in r(). Specifically, if the by() option is not used, concord saves:

S_1	r(N)	number of observations compared	S_7	r(z_tr_ul)	upper CI limit (z-transform)
S_2	r(rho_c)	concordance correlation coefficient, $\hat{\rho}_c$	S_8	r(C_b)	bias-correction factor, $C_b$
S_3	r(se_rho_c)	standard error of $\hat{\rho}_c$ , $\sigma_{\hat{\rho}_c}$	S_9	r(diff)	mean difference
S_4	r(asym_ll)	lower CI limit (asymptotic)	S_10	r(sd_diff)	standard deviation of mean difference
S_5	r(asym_ul)	upper CI limit (asymptotic)	S_11	r(LOA_11)	lower limit-of-agreement value
S_6	r(z_tr_11)	lower CI limit (z-transform)	S_12	r(LOA_ul)	upper limit-of-agreement value

## References

Bland, J. M. and D. G. Altman. 1986. Statistical methods for assessing agreement between two methods of clinical measurement. Lancet I: 307-310.

-----. 1995. Comparing methods of measurement: why plotting difference against standard is misleading. Lancet 346: 1085-1087.

Lin, L. I-K. 1989. A concordance correlation coefficient to evaluate reproducibility. Biometrics 45: 255-68.

- Steichen, T. J. and N. J. Cox. 1998a. sg84: Concordance correlation coefficient. Stata Technical Bulletin 43: 35–9. Reprinted in Stata Technical Bulletin Reprints, vol. 8, pp. 137–143.
- —. 1998b. sg84.1: Concordance correlation coefficient, revisited. Stata Technical Bulletin 45: 21–23. Reprinted in Stata Technical Bulletin Reprints, vol. 8, pp. 143–145.

sg116.1	Update to hotdeck imputation						
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Abstract: Two additional options have been added to the hotdeck command.

Keywords: Hotdeck imputation method.

Two additional options have been added to the hotdeck command introduced in Mander and Clayton (1999).

#### New options

seed(#) specifies the random number generator seed.

infiles(*filename filename ...*) specifies a list of files that have missing values replaced by imputed values. The infiles option allows the user to analyze several imputed datasets that have been created by other programs.

#### Reference

Mander, A. and D. Clayton. 1999. sg116: Hotdeck imputation. Stata Technical Bulletin 51: 32-34.

sg120.2	Correction to roccomp command

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In STB-52 (Cleves 1999), I introduced a series of commands for performing Receiver Operating Characteristic (ROC) analysis on rating and discrete classification data.

A bug was discovered in the roccomp program when more than two modalities were being compared and the modalities were not specified in alphabetical order. The output table reordered the modality variable names placing them in alphabetical order. This could result in the wrong modalities being compared and incorrect significant probabilities reported. This has been corrected. The output table will now present results for each modality in the same order as specified on the command line.

## Reference

Cleves, M. 1999. sg120: Receiver Operating Characteristic (ROC) analysis. Stata Technical Bulletin 52: 19-31.

sg130	Box–Cox regression models
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Abstract: This article describes the boxcox2 command which obtains maximum likelihood estimates for the parameters from any of four distinct Box-Cox regression models. The article also includes a brief introduction to the four Box-Cox regression models. Several examples are used to illustrate how this command can be run and how to interpret the output.

Keywords: Box-Cox regression, nonlinear regression, flexible functional form, specification test.

## Syntax

boxcox2 depvar [indepvars] [weight] [if exp] [in range] [, model(<u>lhs</u>only|<u>rhs</u>only|<u>lam</u>bda|theta)
notrans(varlist) lrtest from(init\_specs) noconstant nolog nologlr iterate(#) level(#) ]

fweights, and iweights are allowed; see [U] 14.1.6 weight.

boxcox2 shares the features of all estimation commands; see [U] 23 Estimation and post-estimation commands.

## Syntax for predict

```
predict [type] newvarname [if exp] [in range] [, { yhat | xbt | residuals } ]
These statistics are available both in and out of sample; type predict ... if e(sample) ... if wanted only for the estimation sample.
```

#### Description

boxcox2 finds the maximum likelihood estimates of the parameter(s) of the Box-Cox transform, the coefficients on the independent variables, and the standard deviation of the normally distributed errors for a model in which *depvar* is regressed on *indepvars*. The user has the option of estimating

Option	Estimates
lhsonly	$y_j^{( heta)} = eta_1 x_{1j} + eta_2 x_{2j} + \dots + eta_k x_{kj} + \epsilon_j$
rhsonly	$y_j = eta_1 x_{1j}^{(\lambda)} + eta_2 x_{2j}^{(\lambda)} + \dots + eta_k x_{kj}^{(\lambda)} + \epsilon_j$
rhsonly notrans()	$y_j = \beta_1 x_{1j}^{(\lambda)} + \beta_2 x_{2j}^{(\lambda)} + \dots + \beta_k x_{kj}^{(\lambda)} + \gamma_1 z_{1j} + \gamma_2 z_{2j} + \dots + \gamma_l z_{lj} + \epsilon_j$
lambda	$y_j^{(\lambda)} = eta_1 x_{1j}^{(\lambda)} + eta_2 x_{2j}^{(\lambda)} + \dots + eta_k x_{kj}^{(\lambda)} + \epsilon_j$
lambda notrans()	$y_j^{(\lambda)} = \beta_1 x_{1j}^{(\lambda)} + \beta_2 x_{2j}^{(\lambda)} + \dots + \beta_k x_{kj}^{(\lambda)} + \gamma_1 z_{1j} + \gamma_2 z_{2j} + \dots + \gamma_l z_{lj} + \epsilon_j$
theta	$y_j^{( heta)} = eta_1 x_{1j}^{(\lambda)} + eta_2 x_{2j}^{(\lambda)} + \dots + eta_k x_{kj}^{(\lambda)} + \epsilon_j$
theta notrans()	$y_j^{(\theta)} = \beta_1 x_{1j}^{(\lambda)} + \beta_2 x_{2j}^{(\lambda)} + \dots + \beta_k x_{kj}^{(\lambda)} + \gamma_1 z_{1j} + \gamma_2 z_{2j} + \dots + \gamma_l z_{lj} + \epsilon_j$

Any transformed variable must be strictly positive.

Note: this command estimates a superset of the models accommodated by the boxcox command of official Stata. See [R] **boxcox** for information on the official command.

#### Options

model(lhsonly|rhsonly|lambda|theta) specifies which of the four models to fit.

model(lhsonly) applies the Box-Cox transform to depvar only. model(lhsonly) is the default value.

model(rhsonly) causes the transform to be applied to the *indepvars* only.

model(lambda) causes the transform to be applied to both *depvar* and *indepvars*, and they are transformed by the same parameter.

model(theta) causes the transform to be applied to both *depvar* and *indepvars*, but this time each side is transformed by a separate parameter.

notrans(varlist) specifies that the variables in varlist are to be included as nontransformed independent variables.

Irtest specifies that a likelihood-ratio test of significance is to be performed and reported for each independent variable.

from() allows the user to specify the initial values for Box-Cox transformation parameter(s); see [R] maximize.

Initial value specification
from( $\theta_0$ , copy)
from( $\lambda_0$ , copy)
from( $\lambda_0$ , copy)
from( $\lambda_0 \ \theta_0$ , copy)

noconstant suppresses the constant term (intercept) in the model.

nolog suppresses the iteration log when estimating the full model.

- nologlr suppresses the iteration log when estimating the restricted models required by the lrtest option. If nologlr is specified when lrtest is not, then it is ignored.
- iterate(#) specifies the maximum number of iterations that the maximum likelihood optimizer will undertake in search of a solution.
- level(#) specifies the confidence level, in percent, for confidence intervals. The default is level(95) or as set by set level; see [U] 23.5 Specifying the width of confidence intervals.

## **Options for predict**

yhat calculates the predicted value of y.

xbt, the default, calculates the "linear" prediction. For all the models except model(lhsonly), all the *indepvars* are transformed. residuals calculates the residuals after the predicted value of y has been subtracted from the actual value.

## Remarks

The Box-Cox transform

$$y^{(\lambda)} = \frac{y^{\lambda} - 1}{\lambda}$$

has been widely used in applied data analysis. Box and Cox (1964) developed the transformation and argued that the transformation could make the residuals more closely normal and less heteroscedastic. Cook and Weisberg (1982) discuss the transform in this light. Since the transform embeds several popular functional forms, it has received some attention as a method for testing functional forms. In particular,

$$y^{(\lambda)} = \begin{cases} y-1 & \text{if } \lambda = 1\\ \ln(y) & \text{if } \lambda = 0\\ 1-1/y & \text{if } \lambda = -1 \end{cases}$$

Davidson and MacKinnon (1993) discuss this use of the transform. Atkinson (1985) also gives a good general treatment.

#### Theta model

boxcox2 obtains the maximum likelihood estimates of the parameters for four different models. The most general of the models, the theta model, is

$$y_{j}^{(\theta)} = \beta_{0} + \beta_{1} x_{1j}^{(\lambda)} + \beta_{2} x_{2j}^{(\lambda)} + \ldots + \beta_{k} x_{kj}^{(\lambda)} + \gamma_{1} z_{1j} + \gamma_{2} z_{2j} + \cdots + \gamma_{l} z_{lj} + \epsilon_{j}$$

where  $\epsilon \sim N(0, \sigma^2)$ . Here the dependent variable y is subject to a Box-Cox transform with parameter  $\theta$ . Each of the *indepvars*  $x_1, x_2, \ldots, x_k$  is transformed by a Box-Cox transform with parameter  $\lambda$ . The  $z_1, z_2, \ldots, z_l$ , specified in the notrans() option, are independent variables that are not transformed.

Box and Cox (1964) argued that this transformation would leave behind residuals that more closely resemble a normal distribution than those produced by a simple linear regression model. Users should bear in mind that the normality of  $\epsilon$  is assumed and that boxcox2 obtains maximum likelihood estimates of the k + l + 4 parameters under this assumption. boxcox2 does not choose  $\lambda$  and  $\theta$  so that the residuals are approximately normally distributed. Users interested in this type of transformation to normality should see the official Stata commands lnskew0 and bcskew0 in [R] lnskew0. However, these commands work on a more restrictive model in which none of the independent variables are transformed.

## Example

Consider an example using the auto data.

. boxcox2 Estimating	mpg we g compa	ight pı rison n	rice, n nodel	otra	ns(foreign)	model(	(theta)	lrtest	t	
Iteration	0: 1	og like	elihood	l = -	234.39434					
Iteration	1: 1	og like	elihood	. = -	228.26891					
Iteration	2: 1	og like	elihood	. = -	228.26777					
Iteration	3: 1	og like	elihood	1 = -	228.26777					
Estimating	g full :	model								
Iteration	0: 1	og like	elihood	. = -	194.13727					
Iteration	1: 1	og like	elihood	. = -	184.34212					
Iteration	2: 1	og like	elihood	L = -	180.18783					
Iteration	3: 1	og like	elihood	L =	-177.5195					
Iteration	4: 1	og like	elihood	L = -	176.08846					
Iteration	5: 1	og like	elihood	L = -	175.67353					
Iteration	6: 1	og like	elihood	. = -	175.67343					
Iteration	7: 1	og like	elihood	. = -	175.67343					
Estimating	g compa	rison n	nodels	for	LR tests					
Iteration	0: 1	og like	elihood	l = -	179.58214					
Iteration	1: 1	og like	elihood	l = -	177.59036					
Iteration	2: 1	og like	elihood	l = -	177.58739					
Iteration	3: 1	og like	elihood	l = -	177.58739					
Iteration	0: 1	og like	elihood	[ = -	203.92855					
Iteration	1: 1	og like	elihood	. = -	201.30202					
Iteration	2: 1	og like	elihood	. = -	201.18246					
Iteration	3: 1	og like	elihood	. = -	201.18233					
Iteration	4: 1	og like	elihood	. = -	201.18233					
Ttomation	0. 1	- 0			179 92700					
Iteration	1. 1	og like	libood	L	175 00405					
Iteration	1: I 0. 1	og like	libood	L	175.90405					
Iteration	2. I 2. I	og like		. — I — _	175 07021					
Iteration	J. I	OR IIV	er moot	. –	110.01001					
								<u> </u>		
						N	Jumber	of obs	=	74
Iom likoli	bood -	175 4	27242			N I	Jumber LR chi2	of obs (4)	=	74 105.19
Log likeli	ihood =	-175.0	67343			N I F	lumber .R chi2 'rob >	of obs (4) chi2	= = =	74 105.19 0.000
Log likeli	ihood =	-175.6	67343 			N I F	lumber .R chi2 ?rob >	of obs (4) chi2	= = =	74 105.19 0.000
Log likeli 	ihood =	-175.0  Coef.	57343  Std.	Err.	Z	N I F P> z	lumber .R chi2 ?rob >	of obs (4) chi2 [95% (	= = = Conf	74 105.19 0.000 
Log likeli 	lhood =   .76	-175.0  Coef.  01691	57343  Std. 	Err. 991	z 1.209	N I F P> z  0.227	lumber .R chi2 ?rob >  / /	of obs (4) chi2 [95% ( 47264	= = Conf 464	74 105.19 0.000 
Log likeli 	ihood =  .76 71	-175.0  Coef.  01691 89315	67343  Std. .6289 .3244	Err. 991 439	z 1.209 -2.216	N I F P> z  0.227 0.027	lumber .R chi2 ?rob >  / 7	of obs (4) chi2 [95% ( 47264 -1.354	= = Conf. 464 483	74 105.19 0.000 
Log likeli 	ihood = 	-175.0  Coef.  01691 89315	57343 Std. .6289 .3244	Err. 991 439	z 1.209 -2.216	N I P> z  0.227 0.027	Jumber .R chi2 ?rob >  / 7 7	of obs (4) chi2 [95% ( 47264 -1.354	= = Conf. 464 483	74 105.19 0.000 Interval] 1.992985 0830332
Log likeli + /lambda   /theta   Estimates	ihood = 	-175.0 Coef. 01691 89315  le-var:	57343 Std. .6289 .3244 iant pa	Err. 991 439 	z 1.209 -2.216 ters	N I P> z  0.227 0.027	Jumber .R chi2 'rob >  7 7	of obs (4) chi2 [95% ( 47264 -1.354	= = 2 Conf 464 483	74 105.19 0.000 Interval] 1.992985 0830332
Log likeli + /lambda   /theta   Estimates	ihood = .76 71 of sca	-175.6  Coef.  01691 89315  le-var:  Coef.	57343 Std. .6289 .3244 iant pa	Err. 991 439 	z 1.209 -2.216 ters P>chi2(df	N I F P> z  0.227 0.027	Jumber JR chi2 Yrob >	of obs (4) chi2 [95% ( 47264 -1.354	= = Conf 464 483	74 105.19 0.000 Interval] 1.992985 0830332
Log likeli 		-175.0 Coef. 01691 89315  le-var: Coef.	57343 Std. .6289 .3244 iant pa chi2(	Err. 9991 439 	z 1.209 -2.216 ters P>chi2(df	N I F P> z  0.227 0.027	<pre>Jumber .R chi2 Prob &gt; 7 7 7 9 0 f chi2</pre>	of obs (4) chi2 [95% ( -1.354	= = Conf. 464 483	74 105.19 0.000 Interval] 1.992985 0830332
Log likeli //lambda   //heta   Estimates		-175.0 Coef. 01691 89315  le-var:  Coef.	57343 Std. .6289 .3244 iant pa 	Err. 991 439 	z 1.209 -2.216 ters P>chi2(df	N I F P> z  0.227 0.027	Jumber .R chi2 Prob >  7 7 7 9 0f chi2	of obs (4) chi2  47264 -1.354	= = Conf. 464 483	74 105.19 0.000 Interval] 1.992985 0830332
Log likeli 		-175.0 Coef.  01691 89315  le-var:  Coef.  14338	57343 Std. .6289 .3244 	Err. 991 439 	z 1.209 -2.216 ters P>chi2(df) 0.050	N I F P> z  0.227 0.027	Jumber .R chi2 Prob > 	of obs (4) chi2  4726 -1.354	= = Conf. 464 483	74 105.19 0.000 Interval] 1.992985 0830332
Log likeli 		-175.0  Coef.  01691 89315  le-var:  Coef.  14338 77399	57343 Std. .6289 .3244 iant pa chi2( 3.8	Err. 991 439 	z 1.209 -2.216 ters P>chi2(df 0.050	N I P> z  0.227 0.027 0.027	Jumber .R chi2 Prob > 	of obs (4) chi2  95% ( -1.354 -1.354	= = Conf. 464 483	74 105.19 0.000 
Log likeli /lambda   /theta   		-175.0  Coef.  01691 89315  le-var:  Coef.  14338 77399	57343 Std. .6289 .3244 iant pa chi2( 3.8	Err. 9991 439 	z 1.209 -2.216 ters P>chi2(df 0.050	N I P> z  0.227 0.027	Jumber .R chi2 Prob > 	of obs (4) chi2  47264 -1.354	= = Conf. 464 483	74 105.19 0.000 
Log likeli /lambda   /theta   Estimates Notrans   foreign    Trans		-175.6 Coef.  01691 89315  le-var:  Coef.  14338 77399 	57343 Std. .6289 .3244 iant pa chi2( 3.8	Err. 991 439  df) 	z 1.209 -2.216 ters P>chi2(df) 0.050	N I P> z  0.227 0.027 0.027	Jumber R chi2 Prob > 7 7 of chi2	of obs (4) chi2  47264 -1.354	= = Conf. 464 483	74 105.19 0.000 Interval] 1.992985 0830332
Log likeli //lambda //theta Estimates Notrans foreign  Trans weight		-175.0 Coef.  01691 89315  Coef.  14338 77399  00239	57343 Std. .6289 .3244 iant pa chi2( 3.8 51.0	Err 991 439  df)  228 	z 1.209 -2.216 ters P>chi2(df) 0.050 0.000	N I F P> z  0.227 0.027	Jumber R chi2 Prob > 7 7 of chi2	of obs (4) chi2 	= = Conf. 464 483	74 105.19 0.000 
Log likeli /lambda   /lambda   /theta   Estimates 		-175.0 Coef.  01691 89315  le-var: Coef. 77399  14338 77399  00239 8e-06	57343 Std. .6289 .3244 iant pa chi2( 3.8 51.0 0.6	Err 991 439  df)  228  18 12	z 1.209 -2.216 ters P>chi2(df) 0.050 0.000 0.434	N I F P> z  0.227 0.027 0.027	Jumber R chi2 Prob > 	of obs (4) chi2 	= = = Conf. 464 483	74 105.19 0.000 [. Interval] 1.992985 0830332
Log likeli /lambda   /lambda   /theta   Estimates Notrans   foreign   _cons   Trans   weight   price		-175.0 Coef.  14338 77399  100239 8e-06 	57343 Std. .6289 .3244 	Err. 991 439  df)  28  18 12	z 1.209 -2.216 ters P>chi2(df 0.050 0.000 0.434	N I F P> z  0.227 0.027 0.027	Jumber R chi2 Prob > of chi2	of obs (4) chi2  47264 -1.354	= = = Conf. 464 483	74 105.19 0.000 Interval] 1.992985 0830332
Log likeli 		-175.0 Coef.  14338 77399  14338 77399  00239 8e-06  38489	57343 Std. .6289 .3244 	Err. 991 439  df)  28  18 12	z 1.209 -2.216 ters P>chi2(df) 0.050 0.000 0.434	N I F P> z  0.227 0.027 0.027	Jumber R chi2 Prob >	of obs (4) chi2  47264 -1.354	= = = Conf. 464 483	74 105.19 0.000 Interval] 1.992985 0830332
Log likeli /lambda   /theta   Estimates Notrans   foreign    Trans   weight   price   		-175.0 Coef.  01691 89315  Coef.  14338 77399  00239 8e-06  38489 	57343 Std. .6289 .3244 iant pa chi2( 3.8 51.0 0.6	Err. 991 439  rame df)  28  18 12 	z 1.209 -2.216 ters P>chi2(df 0.050 0.000 0.434	N I F P> z  0.227 0.027	Jumber R chi2 Prob > 7 7 0f chi2 1	of obs (4) chi2  47264 -1.354	= = = Conf: 464 483	74 105.19 0.000  1nterval]  1.992985 0830332
Log likeli /lambda   /theta   Estimates Notrans   foreign   _cons   Trans   weight   price   /sigma   	Lhood = 	-175.0  Coef.  149315  le-var:  Coef.  14338 77399  14338 77399  00239 8e-06  38489 	57343 Std. .6289 .3244 iant pa chi2( 3.8 51.0 0.6	Err. 991 439  df)  28  18 12  18 12 	z 1.209 -2.216 ters P>chi2(df 0.050 0.000 0.434	N I F P> z  0.227 0.027	Jumber R chi2 Prob > of chi2	of obs (4) chi2  4726 -1.354	= = Conf. 464 483	74 105.19 0.000  1.1992985 0830332
Log likeli /lambda   /theta   Estimates Notrans   foreign   _cons   Trans   weight   price   		-175.6 Coef.  01691 89315  Coef.  14338 77399  00239 8e-06  38489  38489  F	57343 Std. .6289 .3244 iant pa chi2( 3.8 51.0 0.6 	Err. 991 439 df) 28 118 12  ted	z 1.209 -2.216 ters P>chi2(df 0.050 0.000 0.434	N I P> z  0.227 0.027	Jumber R chi2 Prob > 	of obs (4) chi2  47264 -1.354 	= = 464 483	74 105.19 0.000 
Log likeli /lambda /lambda /theta Estimates Notrans foreign _cons Trans weight price /sigma Test HO:		-175.0 Coef.  le-var:  Coef.  14338 77399  00239 8e-06  38489  38489  Base  Satas 	57343 Std. .6289 .3244 iant pa chi2( 3.8 51.0 0.6 	Err. 991 439 df) 28  18 12  ted ihoo	z 1.209 -2.216 ters P>chi2(df) 0.050 0.000 0.434 d X~ch:	N I F P> z  0.227 0.027	Jumber R chi2 Prob > 7 7 of chi2	of obs (4) chi2 47264 -1.354 	= = 	74 105.19 0.000 
Log likeli /lambda /lambda /theta Estimates Notrans foreign  Trans weight price /sigma Test HO: theta=lamb	hood = 	-175.0 Coef.  le-var:  Coef.  00239 8e-06  38489  38489  1 log	57343 Std. .6289 .3244 iant pa chi2( 3.8 51.0 0.6 	Err. 991 439 df) 28 12 18 12  ted ihoo  479	z 1.209 -2.216 ters P>chi2(df) 0.050 0.000 0.434 d X~ch 11.9	N I F P> z  0.227 0.027 0.027 1 1 1 1 1	Jumber R chi2 Prob > of chi2	of obs (4) chi2 47264 -1.354 	= = 2 Conf. 464 483	74 105.19 0.000 
Log likeli //lambda // //lambda // Estimates Estimates Notrans // foreign //  Trans // weight // price // /sigma // Test HO: theta=lambttheta=lambttheta=lambt	Lhood = 	-175.0 Coef.  le-var:  Coef.  14338 77399  00239 8e-06  38489  Base  10g 10g	57343 Std. .6289 .3244 iant pa chi2( 3.8 51.0 0.6 Std. 1.0 0.6 	Err. 991 439  df)  28  18 12  18 12  18 12  18 12  18 12  479 406	z 1.209 -2.216 ters P>chi2(df) 0.050 0.000 0.434 d X~ch 11.9 5.11	N I P> z  0.227 0.027 0.027 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Jumber R chi2 Prob > of chi2 Pr Pr 0 0	of obs (4) chi2 47264 -1.354 	= = 	74 105.19 0.000  1.992985 0830332
Log likeli 	Lhood = 	-175.0 Coef.  le-var:  Coef. 14338 77399  00239 8e-06  38489  10g 10g 10g	57343 Std. .6289 .3244 	Err. 991 439  df)  28  18 12  18 12  ted ihoo  ted 2479 406 4727	z 1.209 -2.216 ters P>chi2(df) 0.050 0.000 0.434 d X~ch: 11.9 5.1: 36.9:	N I F P> z  0.227 0.027 0.027 0.027 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Jumber R chi2 Prob > 	of obs (4) chi2 47264 -1.354 	= = 2 464 483	74 105.19 0.000 Interval] 1.992985 0830332

The output is composed of the iteration logs and three distinct tables. The first table contains a standard header for a maximum likelihood estimator and a standard output table for the Box-Cox transform parameters. The second table contains the estimates of the scale-variant parameters. The third table contains the output from likelihood-ratio tests on three standard functional form specifications.

If we were to interpret this output, the right-hand-side transformation does not significantly add to the regression while the left-hand-side transformation makes the 5% but not the 1% cutoff. price is certainly not significant and foreign lies right on the 5% cutoff. weight is clearly significant. The output also says that both the linear and multiplicative inverse specifications are strongly rejected. A natural log specification can be rejected at the 5% but not the 1% level.

## **Technical Note**

Spitzer (1984) showed that the Wald statistics of whether the coefficients of the right-hand-side variables, transformed or untransformed, are significantly different than zero are not invariant to changes in the scale of the transformed dependent variable. Davidson and MacKinnon (1993) also discuss this point. It is worth noting that this problem is an example of the manipulability of Wald statistics in nonlinear models. Lafontaine and White (1986) analyze this problem numerically and Phillips and Park (1988) analyze it analytically using Edgeworth expansions. See Drukker (2000) for a more detailed discussion of this issue. Since the parameter estimates and their Wald tests are not scale invariant, no Wald tests or confidence intervals are reported for these parameters. However, when the lrtest option is specified, likelihood-ratio tests are performed and reported. Schlesselman (1971) showed that, if a constant is included in the model, then the parameter estimates of the Box–Cox transforms are scale invariant. For this reason, it is highly recommended that the no constant option not be used.

The lrtest option does not perform a likelihood-ratio test on the constant. Hence, no value for this statistic is reported. Unless the data are properly scaled, the restricted model frequently does not converge. For this reason, no likelihood-ratio test on the constant is performed by the lrtest option. However, if a user has a special interest in performing this test, then it can be done by estimating the constrained model separately. If problems with convergence are encountered, rescaling the data by their means may help.

## Lambda model

A less general model than the one above is called the lambda model. It specifies that the same parameter be used in both the left-hand side and right-hand side transformations. Specifically,

$$y_{j}^{(\lambda)} = \beta_{0} + \beta_{1} x_{1j}^{(\lambda)} + \beta_{2} x_{2j}^{(\lambda)} + \dots + \beta_{k} x_{kj}^{(\lambda)} + \gamma_{1} z_{1j} + \gamma_{2} z_{2j} + \dots + \gamma_{l} z_{lj} + \epsilon_{j}$$

where  $\epsilon \sim N(0, \sigma^2)$ . Here the *depvar* variable y and each of the *indepvars*  $x_1, x_2, \ldots, x_k$  are transformed by a Box-Cox transform with the common parameter  $\lambda$ . Again, the  $z_1, z_2, \ldots, z_l$  are independent variables that are not transformed.

#### Example

Again using the auto data we have

. boxcox2 mpg weight price, notrans(foreign) model(lambda) lrtest nolog nologlr Estimating comparison model Estimating full model Estimating comparison models for LR tests

Log likeli	ihood = -177.	16463		Number LR chi2 Prob >	of obs = (3) = chi2 =	74 102.21 0.000
mpg	Coef.	Std. Err.	z	P> z	[95% Conf	. Interval]
/lambda	3188704	.2185908	-1.459	0.145	7473006	.1095597
Estimates	of scale-var Coef.	iant paramet  chi2(df)	ers P>chi2(df)	df of chi2		
Notrans foreign _cons	0271361 15.11529	1.924	0.165	1		
Trans weight price	-3.964759 5849437	48.047 2.478	0.000 0.115	1 1		
/sigma	.0748609					

Test HO:	Restricted log likelihood	LR statistic X~chi2	P-Value Pr > chi2
lambda = -1	-181.64479	8.96	0.003
lambda = 0	-178.2406	2.15	0.142
lambda = 1	-194.13727	33.95	0.000

The options nolog and nologlr were specified to suppress the iteration logs. Aside from this change, the output of this example has the same outline as that of the previous one. The most important change is in the first table. Since the requested model has only one Box–Cox transform parameter, only one is reported. The interpretation is similar to the previous case.

## Left-hand-side only model

More restrictive still than a common transformation parameter is transforming the dependent variable only. Since the dependent variable is on the left hand side of the equation, this model is known as the lhsonly model. In this case, one is estimating the parameters of the model

$$y_i^{(\theta)} = \beta_0 + \beta_1 x_{1j} + \beta_2 x_{2j} + \dots + \beta_k x_{kj} + \epsilon_j$$

where  $\epsilon \sim N(0, \sigma^2)$ . In this case only the *depvar*, y, is transformed by a Box-Cox transform with the parameter  $\theta$ . Note that the  $z_1, z_2, \ldots, z_L$  have been dropped from the specification. Since the *indepvars*  $x_1, x_2, \ldots, x_K$  are not transformed, the  $z_1, z_2, \ldots, z_L$  are superfluous.

This is the model that is estimated by Stata's boxcox command. Even here, boxcox2 offers some advantages over boxcox. In particular, one can easily obtain likelihood-ratio tests of the significance of the independent variables. In contrast, boxcox offers Wald statistics that use variance estimates of the coefficients which are conditional on  $\theta$ . This difference is important. Spitzer (1984) shows that the variance estimates conditional on  $\theta$  will underestimate the true variance.

#### Example

In this example, mpg is again hypothesized to be a function of weight, price and foreign in a Box-Cox model in which only mpg is subject to the transform.

. boxcox2 mpg weight price foreign, model(lhs) lrtest nolog nologlr Estimating comparison model Estimating full model Estimating comparison models for LR tests

Log likel	ihood = -175.	74705		Number o LR chi2 Prob > o	of obs (3) chi2	= = =	74 105.04 0.000
mpg	   Coef.	Std. Err.	Z	P> z	[95% 0	Conf.	Interval]
/theta	7826999	.281954	-2.776	0.006	-1.335	532	2300802
Estimates	of scale-var	iant parame	ters				
	Coef.	chi2(df)	P>chi2(df)	df of chi2			
Notrans	+						
weight	0000294	58.056	0.000	1			
price	-4.66e-07	0.469	0.493	1			
foreign	0097564	4.644	0.031	1			
_cons	1.249845						
/sigma 	.013249						
 Test	Restri	cted LR	statistic	P-Value			
HO:	log like	lihood	X~chi2	Pr > chi2			
theta = -	1 -176.0	4312	0.59	0.442			
theta =	0 -179.5	4104	7.59	0.006			
theta =	1 -194.1	3727	36.78	0.000			

It is worth noting that this model rejects both the linear and log specification of mpg but fails to reject that 1/mpg is linear in the independent variables. These findings are in line with the what an engineer would have expected *ex ante*. In engineering terms, gallons per mile represent actual energy consumption and energy consumption should be approximately linear in weight.

## **Right-hand-side only model**

The fourth model leaves the *depvar* alone and transforms a subset of the *indepvars* using the parameter  $\lambda$ . This is the **rhsonly** model. In this model the *depvar*, y, is given by

$$y_{j} = \beta_{0} + \beta_{1} x_{1j}^{(\lambda)} + \beta_{2} x_{2j}^{(\lambda)} + \ldots + \beta_{k} x_{kj}^{(\lambda)} + \gamma_{1} z_{1j} + \gamma_{2} z_{2j} + \cdots + \gamma_{l} z_{lj} + \epsilon_{j}$$

where  $\epsilon \sim N(0, \sigma^2)$ . Here each of the *indepvars*  $x_1, x_2, \ldots, x_k$  are transformed by a Box–Cox transform with the parameter  $\lambda$ . Again, the  $z_1, z_2, \ldots, z_l$  are independent variables that are not transformed.

#### Example

Here is an example with the rhsonly model. In this example, price and foreign are not included in the list of covariates. (You are invited to use the auto data and check that they fare no better here than above.)

```
. boxcox2 mpg weight, model(rhs) lrtest nolog nologlr
Estimating Full Model
Estimating comparison models for LR tests
Comparison model for LR test on weight is a linear regression
Lambda is not identified in the restricted model
```

Log likelih	.ood = -192.9	94368		Numb LR c Prob	er of obs hi2(2) o > chi2	=	74 82.90 0.000
mpg	Coef.	Std. Err.	Z	P> z	[95% Con	nf.	Interval]
/lambda	4460916	.6551107	-0.681	0.496	-1.730085	5	.8379017

#### Estimates of Scale Variant Parameters

	Coef.	chi2(df	) P>chi2(d:	f) df of ch	i2
Notrans _cons	1359.092	2			
Trans weight	-614.3874	82.901	0.000	2	
/sigma	3.281854	l 			
Test HO:	Resti log lik	ricted Kelihood	LR statistic X~chi2	P-Valu Pr > ch	 e i2
lambda = lambda = lambda =	-1 -193 0 -193 1 -195	3.2893 17892 38869	0.69 0.47 4.89	0.406 0.493 0.027	

The interpretation of the output is similar to all the cases above, except for one caveat. As requested, a likelihood-ratio test was performed on the lone independent variable. However, when it is dropped to form the constrained model, the comparison model is not a right-hand-side only Box–Cox model, but rather a simple linear regression on a constant model. When weight is dropped, there are no longer any transformed variables. Hence,  $\lambda$  is not identified and it must also be dropped. This process leaves a linear regression on a constant as the "comparison model". It also implies that the test statistic has 2 degrees of freedom instead of 1. At the top of the output, there is a more concise warning which informs the user of this point.

#### Technical Note

A similar identification issue can also arise in the lambda and theta models when only one independent variable is specified. In these cases, warnings also appear on the output to remind the user.

## **Saved Results**

boxcox2 saves in e():

Scalars			
e(N)	number of observations	e(chi2)	LR statistic of full vs comparison
e(11)	log likelihood	e(110)	log likelihood of the restricted model
e(df_m)	full model degrees of freedom	e(df_r)	restricted model degrees of freedom
e(11_t1)	log likelihood of model when $\lambda = \theta = 1$	e(chi2_t1)	LR statistic of $\lambda = \theta = 1$ vs full model
e(p_t1)	<i>p</i> -value of $\lambda = \theta = 1$ vs full model	e(ll_tm1)	log likelihood of model when $\lambda = \theta = -1$
e(chi2_tm1)	LR statistic of $\lambda = \theta = -1$ vs full model	e(p_tm1)	<i>p</i> -value of $\lambda = \theta = -1$ vs full model
e(11_t0)	log likelihood of model when $\lambda = \theta = 0$	e(chi2_t0)	LR statistic of $\lambda = \theta = 0$ vs full model
e(p_t0)	<i>p</i> -value of $\lambda = \theta = 0$ vs full model	e(ic)	number of iterations
e(rc)	return code		
Macros			
e(cmd)	boxcox2	e(ntrans)	yes if there were nontransformed indepvars
e(model)	model estimated	e(predict)	program used to implement predict
e(chi2type)	LR	e(lrtest)	lrtest if requested
e(depvar)	name of dependent variable	e(wtype)	weight type
e(wexp)	weight expression		
Matrices			
e(b)	coefficient vector	e(V)	variance-covariance matrix of the
e(df)	degrees of freedom of LR tests on indepvars,		estimators (see note below)
	if requested	e(pm)	p-values for LR tests on indepvars, if requested
e(chi2m)	LR statistics for tests on <i>indepvars</i> , if requested		

Functions

e(sample) marks estimation sample

Note that e(V) contains all zeros except for the element(s) that correspond to the parameter(s) of the Box-Cox transform.

## **Methods and Formulas**

boxcox2 is implemented as an ado-file.

In the internal computations

$$y^{(\lambda)} = \begin{cases} rac{y^{\lambda} - 1}{\lambda} & ext{if } |\lambda| > 10^{-10} \\ \ln(y) & ext{otherwise} \end{cases}$$

The unconcentrated log likelihood for the theta model is

$$\ln L = \left(\frac{-N}{2}\right) \left(\ln(2\pi) + \ln(\sigma^2)\right) + (\theta - 1)\sum_{i}^{N} \ln(y_i) - \left(\frac{1}{2\sigma^2}\right) \text{SSR}$$

where

$$SSR = \sum_{i}^{N} (y_{i}^{(\theta)} - \beta_{0} + \beta_{1} x_{i1}^{(\lambda)} + \beta_{2} x_{i2}^{(\lambda)} + \ldots + \beta_{k} x_{ik}^{(\lambda)} + \gamma_{1} z_{i1} + \gamma_{2} z_{i2} + \ldots + \gamma_{l} z_{il})^{2}$$

Writing the SSR in matrix form,

$$SSR = (\mathbf{Y}^{(\theta)} - \mathbf{X}^{(\lambda)}\mathbf{b}' - \mathbf{Zg}')'(\mathbf{Y}^{(\theta)} - \mathbf{X}^{(\lambda)}\mathbf{b}' - \mathbf{Zg}')$$

where  $\mathbf{Y}^{(\theta)}$  is an  $N \times 1$  vector of elementwise transformed data,  $\mathbf{X}^{(\lambda)}$  is an  $N \times k$  matrix of elementwise transformed data,  $\mathbf{Z}$  is an  $N \times l$  matrix of untransformed data,  $\mathbf{b}$  is a  $1 \times k$  vector of coefficients, and  $\mathbf{g}$  is a  $1 \times l$  vector of coefficients. Letting

$$\mathbf{W}_{\lambda} = \left( \mathbf{X}^{(\lambda)} \ \mathbf{Z} 
ight)$$

the horizontal concatenation of  $\mathbf{X}^{(\lambda)}$  and  $\mathbf{Z}$ , and

$$\mathbf{d}' = \begin{pmatrix} \mathbf{b}' \\ \mathbf{g}' \end{pmatrix}$$

the vertical concatenation of the coefficients, yields

$$\mathrm{SSR} = (\mathbf{Y}^{( heta)} - \mathbf{W}_{\lambda}\mathbf{d}')'(\mathbf{Y}^{( heta)} - \mathbf{W}_{\lambda}\mathbf{d}')$$

For given values of  $\lambda$  and  $\theta$ , the solutions for d' and  $\sigma^2$  are

$$\widehat{\mathbf{d}}' = (\mathbf{W}_{\lambda}'\mathbf{W}_{\lambda})^{-1}\mathbf{W}_{\lambda}'\mathbf{Y}^{(\theta)}$$

and

$$\widehat{\sigma}^2 = \frac{1}{N} \left( \mathbf{Y}^{\theta} - \mathbf{W}_{\lambda} \widehat{\mathbf{d}}' \right)' \left( \mathbf{Y}^{\theta} - \mathbf{W}_{\lambda} \widehat{\mathbf{d}}' \right)$$

Substituting these solutions into the log-likelihood function yields the concentrated log-likelihood function,

$$\ln L_c = \left(-\frac{N}{2}\right) \left(\ln(2\pi) + 1 + \ln(\widehat{\sigma}^2)\right) + (\theta - 1) \sum_{i}^{N} \ln(y_i)$$

The unconcentrated log likelihood for the lambda model is

$$\ln L = \left(\frac{-N}{2}\right) \left(\ln(2\pi) + \ln(\sigma^2)\right) + (\lambda - 1) \sum_{i}^{N} \ln(y_i) - \left(\frac{1}{2\sigma^2}\right) \text{SSR}$$

where

$$SSR = \sum_{i}^{N} (y_{i}^{(\lambda)} - \beta_{0} + \beta_{1} x_{i1}^{(\lambda)} + \beta_{2} x_{i2}^{(\lambda)} + \ldots + \beta_{k} x_{ik}^{(\lambda)} + \gamma_{1} z_{i1} + \gamma_{2} z_{i2} + \ldots + \gamma_{l} z_{il})^{2}$$

Writing the SSR in matrix form,

$$\mathrm{SSR} = (\mathbf{Y}^{(\lambda)} - \mathbf{X}^{(\lambda)}\mathbf{b}' - \mathbf{Zg}')'(\mathbf{Y}^{(\lambda)} - \mathbf{X}^{(\lambda)}\mathbf{b}' - \mathbf{Zg}')$$

where  $\mathbf{Y}^{(\lambda)}$  is an  $N \times 1$  vector of transformed data and everything else has already been defined. Using  $\mathbf{W}_{\lambda}$  and  $\mathbf{d}$  as defined above, the sum of squared residuals is now

$$\mathrm{SSR} = (\mathbf{Y}^{(\lambda)} - \mathbf{W}_{\lambda}\mathbf{d}')'(\mathbf{Y}^{(\lambda)} - \mathbf{W}_{\lambda}\mathbf{d}')$$

For a given value of  $\lambda$ , the solutions for d' and  $\sigma^2$  are

$$\widehat{\mathbf{d}}' = (\mathbf{W}_\lambda' \mathbf{W}_\lambda)^{-1} \mathbf{W}_\lambda' \mathbf{Y}^{(\lambda)}$$

and

$$\hat{\sigma}^2 = \frac{1}{N} \left( \mathbf{Y}^{\lambda} - \mathbf{W}_{\lambda} \hat{\mathbf{d}}' \right)' \left( \mathbf{Y}^{\lambda} - \mathbf{W}_{\lambda} \hat{\mathbf{d}}' \right)$$

Substituting these solutions into the log-likelihood function yields the concentrated log-likelihood function:

$$\ln L_c = \left(-\frac{N}{2}\right) \left(\ln(2\pi) + 1 + \ln(\widehat{\sigma}^2)\right) + (\lambda - 1) \sum_{i}^{N} \ln(y_i)$$

The unconcentrated log likelihood for the lhsonly model is

$$\ln L = \left(\frac{-N}{2}\right) \left(\ln(2\pi) + \ln(\sigma^2)\right) + (\theta - 1) \sum_{i}^{N} \ln(y_i) - \left(\frac{1}{2\sigma^2}\right) \text{SSR}$$

where

$$SSR = \sum_{i}^{N} (y_{i}^{(\theta)} - \beta_{0} + \beta_{1}x_{i1} + \beta_{2}x_{i2} + \ldots + \beta_{k}x_{ik})^{2}$$

Writing the SSR in matrix form,

$$SSR = (\mathbf{Y}^{(\theta)} - \mathbf{Xb}')'(\mathbf{Y}^{(\theta)} - \mathbf{Xb}')$$

where  $\mathbf{Y}^{(\theta)}$  is an  $N \times 1$  vector of transformed data,  $\mathbf{X}$  is an  $N \times k$  matrix of untransformed data,  $\mathbf{b}$  is a  $1 \times k$  vector of coefficients. For a given value of  $\theta$ , the solutions for  $\mathbf{b}'$  and  $\sigma^2$  are

$$\widehat{\mathbf{b}}' = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{Y}^{(\theta)}$$

and

$$\widehat{\sigma}^{2} = \frac{1}{N} \left( \mathbf{Y}^{(\theta)} - \mathbf{X} \widehat{\mathbf{b}}' \right)' \left( \mathbf{Y}^{(\theta)} - \mathbf{X} \widehat{\mathbf{b}}' \right)$$

Substituting these solutions into the log-likelihood function yields the concentrated log-likelihood function:

$$\ln L_c = \left(-\frac{N}{2}\right) \left(\ln(2\pi) + 1 + \ln(\widehat{\sigma}^2)\right) + (\theta - 1) \sum_{i}^{N} \ln(y_i)$$

The unconcentrated log likelihood for the rhsonly model is

$$\ln L = \left(\frac{-N}{2}\right) \left(\ln(2\pi) + \ln(\sigma^2)\right) - \left(\frac{1}{2\sigma^2}\right) \text{SSR}$$

where

$$SSR = \sum_{i}^{N} (y_{i} - \beta_{0} + \beta_{1} x_{i1}^{(\lambda)} + \beta_{2} x_{i2}^{(\lambda)} + \ldots + \beta_{k} x_{ik}^{(\lambda)} + \gamma_{1} z_{i1} + \gamma_{2} z_{i2} + \ldots + \gamma_{l} z_{il})^{2}$$

Writing the SSR in matrix form,

$$SSR = (\mathbf{Y} - \mathbf{X}^{(\lambda)}\mathbf{b}' - \mathbf{Zg}')'(\mathbf{Y} - \mathbf{X}^{(\lambda)}\mathbf{b}' - \mathbf{Zg}')$$

where **Y** is an  $N \times 1$  vector of untransformed data,  $\mathbf{X}^{(\lambda)}$  is an  $N \times k$  matrix of transformed data, **Z** is an  $N \times l$  matrix of untransformed data, **b** is a  $1 \times k$  vector of coefficients, and **g** is a  $1 \times l$  vector of coefficients. Letting

$$\mathbf{W}_{\lambda} = \left(\mathbf{X}^{(\lambda)} \ \mathbf{Z}
ight)$$

the horizontal concatenation of  $\mathbf{X}^{(\lambda)}$  and  $\mathbf{Z}$ , and

$$\mathbf{d}' = \begin{pmatrix} \mathbf{b}' \\ \mathbf{g}' \end{pmatrix}$$

yields

$$\mathrm{SSR} = (\mathbf{Y} - \mathbf{W}_\lambda \mathbf{d}')' (\mathbf{Y} - \mathbf{W}_\lambda \mathbf{d}')$$

For a given value of  $\lambda$ , the solutions for d' and  $\sigma^2$  are

$$\widehat{\mathbf{d}}' = (\mathbf{W}'_{\lambda}\mathbf{W}_{\lambda})^{-1}\mathbf{W}'_{\lambda}\mathbf{Y}$$

and

$$\widehat{\sigma}^2 = rac{1}{N} \Big( \mathbf{Y} - \mathbf{W}_\lambda \widehat{\mathbf{d}}' \Big)' \left( \mathbf{Y} - \mathbf{W}_\lambda \widehat{\mathbf{d}}' 
ight)$$

Substituting these solutions into the log-likelihood function yields the concentrated log-likelihood function:

$$\ln L_c = \left(-\frac{N}{2}\right) \left(\ln(2\pi) + 1 + \ln(\widehat{\sigma}^2)\right)$$

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sg131	On the manipulability of Wald tests in Box–Cox regression models

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- Abstract: This article illustrates the fact that the value of the Wald Test of the significance of a coefficient on an independent variable in a Box-Cox regression model is not invariant to changes in the scale of any of the transformed variables. The article shows that this result is a special case of the manipulability of the Wald statistic in nonlinear models, a topic that has been treated in the literature by Lafontaine and White (1986) and Phillips and Park (1988). The article considers several candidate methods for dealing with the problem and concludes that using likelihood-ratio tests is the best alternative.
- **Keywords:** Box–Cox regression, nonlinear regression, Wald tests, nonlinear models, scale invariance, scale invariant test statistics, scale variant test statistics.

#### Introduction

This article illustrates the fact that the value of the Wald test of the significance of a coefficient on an independent variable in a Box–Cox regression model is not invariant to changes in the scale of any of the transformed variables. Spitzer (1984) first discovered this fact in a study of Box–Cox regression models. Later, in independent work, Gregory and Veal (1985) and Lafontaine and White (1986) showed that certain classes of nonlinear transformations of a Wald test produce significantly different values and conclusions in a finite sample. Phillips and Park (1988) used Edgeworth expansions to generalize this conclusion to a very general class of nonlinear transformations.

The manipulability of the Wald test of the significance of an independent variable in a Box–Cox regression is a special case of the more general phenomenon that Wald tests are not invariant to nonlinear transforms. This article uses two different Stata commands that perform Box–Cox regression and examples from the auto dataset to illustrate this fact. The first command box has a syntax similar to the new boxcox2 which is documented in the online help and in Drukker (2000). The command box is neither an official Stata command nor a command released in another format, such as the STB. box was written by the author for the purpose of writing this article. Researchers interested in estimating Box–Cox models are encouraged to use boxcox2.

In Box-Cox regressions, some or all of the variables are transformed by the Box-Cox transform which is

$$w^{(\theta)} = \frac{w^{\theta} - 1}{\theta}$$

Box–Cox regressions can take one of four different forms, depending on which variables are transformed. The examples in this article all use the Box–Cox model in which only the dependent variable is transformed. Since the dependent variable appears on the left-hand-side, this model is called the "left-hand-side only model". Specifically, the model estimated in these examples is

$$y_j^{(\theta)} = \beta_0 + \beta_1 x_{1j} + \beta_2 x_{2j} + \dots + \beta_k x_{kj} + \epsilon_j$$

where  $\epsilon \sim N(0, \sigma^2)$ . Although the discussion is focused on this one model, the issues generalize to all four of the models estimated by boxcox2. For an introduction to Box–Cox models, see Davidson and MacKinnon (1993). For a discussion of their implementation in Stata, see Drukker (2000).

#### **Obtaining any Wald statistic**

The variance of the Wald test to nonlinear transforms is the root of the problem. Hence, a good place to begin our investigation is with a simple example of this phenomenon. Consider the following example, which is similar to one given in Lafontaine and White (1986). Running a linear regression of mpg on weight and price, using the auto dataset produces

. regress	mpg price wei	ght				
Source	SS	df	MS		Number of obs =	= 74
Model Residual	+   1595.93249   847.526967	2 797.9 71 11.93	966246 369995		F(2, 71) = Prob > F = R-squared = R-squa	= 66.85 = 0.0000 = 0.6531
Total	2443.45946	73 33.47	720474		Root MSE =	= 0.6434 = 3.455
mpg	Coef.	Std. Err.	t	P> t	[95% Conf. ]	[nterval]
price weight _cons	0000935  0058175   39.43966	.0001627 .0006175 1.621563	-0.575 -9.421 24.322	0.567 0.000 0.000	000418 0070489 - 36.20635	.0002309 0045862 42.67296

Now, let's perform several equivalent tests of whether or not weight is significant in the regression.

```
. test weight
(1) weight = 0.0
      F( 1, 71) = 88.75
           Prob > F = 0.0000
. testnl _b[weight]=0
 (1) _b[weight]=0
             F(1, 71) =
                             88.75
             Prob > F =
                              0.0000
. testnl _b[weight]^2=0
 (1) _b[weight]^2=0
             F(1, 71) =
                             22.19
             Prob > F =
                              0.0000
```

Note that when the same Wald test is performed with test and testnl, the same value of the Wald statistic is obtained. However, when the logically equivalent, but algebraically distinct test of whether or not  $\beta_{weight}^2 = 0$  is performed, the value of the test is approximately a fourth of its original value. As shown in Lafontaine and White (1986, 35), "because the nonlinear form of the Wald statistic stems from a Taylor series approximation, different values and possibly different diagnostics are obtained from the above seeming equivalent tests".

Phillips and Park (1988) used Edgeworth expansions to generalize the previous research. They were able to demonstrate that

Under general conditions Wald statistics which are based upon different but algebraically equivalent forms all have the same asymptotic distribution under the null hypothesis that the restriction holds. However, numerical outcomes of the tests and their finite sample distributions can be substantially different for different forms of the same restrictions.

## Scale-variant Wald statistics in Box–Cox regressions

Spitzer (1984) first discovered that Wald tests of the significance of an independent variable were not invariant to changes in the scale of any transformed variable in a Box–Cox regression. He derives the variance estimator for the coefficients on the right-hand-side independent variables in a Box–Cox regression model in which only the dependent variable is transformed. Spitzer shows analytically that this variance estimator depends on the scale of the dependent variable. He goes on to give numerical examples that show how the value of the Wald test of the significance of the independent variables can be manipulated by changing the scale of the dependent variable.

Consider a similar example using the auto dataset. This example will illustrate the lack of scale-invariance and it will also show how this is a special case of the manipulability of Wald tests via nonlinear restrictions. Begin with a Box–Cox regression in which only the dependent variable is transformed.

```
. box mpg weight price , nolog
Estimating comparison model
Maximizing concentrated likelihood
Maximizing the unconcentrated likelihood
Log likelihood = -178.06886
Mumber of obs = 74
LR chi2(3) = 100.40
Prob > chi2 = 0.0000
```

mpg	Coef.	Std. Err.	z	P> z	[95% Conf	. Interval]
ntrans						
weight	0000263	.0000232	-1.132	0.258	0000718	.0000192
price	-1.34e-06	1.18e-06	-1.135	0.256	-3.66e-06	9.75e-07
_cons	1.272474	.4123654	3.086	0.002	.4642524	2.080695
Ancillary						
theta	7568509	.2901099	-2.609	0.009	-1.325456	1882459
sigma	.0132169	.0116479	1.135	0.256	0096125	.0360462

. test \_b[ntrans: weight]=0

A Wald test of the significance of weight is also performed. Note that this test produces a *p*-value identical to that given in the output table. This value indicates the unlikely diagnostic that weight does not have a statistically significant effect on mpg, at any of the standard test sizes.

Now, rescale mpg to mpg/10 and rerun the same procedure.

```
    gen mpg2=mpg/10
    box mpg2 weight price, nolog
    Estimating comparison model
```

Maximizing concentrated likelihood

Maximizing the unconcentrated likelihood

				Num	ber of obs	=	74
				LR	chi2(3)	=	100.40
Log likeli	hood = -7.67	75588		Pro	b > chi2	=	0.0000
mpg2	Coef.	Std. Err.	z	P> z	[95% Co	nf.	Interval]
ntrans							
weight	0001502	.0000344	-4.365	0.000	000217	7	0000828
price	-7.66e-06	3.61e-06	-2.123	0.034	000014	7	-5.88e-07
_cons	1.042532	.1589603	6.558	0.000	.730975	8	1.354089
Ancillary							
theta	7568511	.2902993	-2.607	0.009	-1.32582	7	1878749
sigma	.0755057	.0169982	4.442	0.000	.042189	8	.1088216

Note that the Wald test in the table now indicates that weight is indeed a statistically significant predictor of mpg/10 at all of the conventional sizes.

Since there is a constant in the model, estimates of the Box–Cox transform parameter and its variance are invariant to any rescaling of the variables. Schlesselman (1971) demonstrated this point analytically. Using this fact, a few lines of algebra show that a rescaling of the dependent variable in a left-hand-side only Box–Cox regression model results in a simple nonlinear transformation of the parameters. Specifically, write the original model as

$$rac{\mathbf{y}^{ heta}-\mathbf{1}}{ heta}=\mathbf{X}\mathbf{b}+\mathbf{e}$$

where y is an  $N \times 1$  vector of observations on the dependent variable,  $\theta$  is the parameter of the Box–Cox transform, X is the  $N \times k$  matrix of observations on the independent variables, b is the  $k \times 1$  vector of coefficients on the independent variables and e is the  $N \times 1$  vector of normally distributed errors. X contains a vector of ones in its first column.

Now, rescale the regression.

$$\frac{\left(\frac{\mathbf{y}}{\mathbf{c}}\right)^{\theta}-1}{\theta}=\mathbf{X}\mathbf{b_s}+\mathbf{e_s}$$

where  $\mathbf{b}_{s}$  is the  $k \times 1$  vector of coefficients in the scaled model. Since estimates of  $\theta$  are invariant to the transform, it needs no subscript. Solving this equation for

$$rac{\mathbf{y}^{ heta}-\mathbf{1}}{ heta}$$

implies that

$$\frac{\mathbf{y}^{\theta}-\mathbf{1}}{\theta} = \frac{\mathbf{c}^{\theta}-\mathbf{1}}{\theta} + \mathbf{c}^{\theta}\mathbf{X}\mathbf{b_s} + \mathbf{c}^{\theta}\mathbf{e_s}$$

the implication being that, except for the constant,

 $\mathbf{b} = \mathbf{c}^{\theta} \mathbf{b}_{\mathbf{s}}$ 

It is easy to verify that this formula works for the example at hand.

. scalar b1=\_b[ntrans: weight]\*10^(\_b[theta: \_cons])
. di b1
-.0000263

This situation is now similar to the example of  $\beta_{\text{weight}}$  and  $\beta_{\text{weight}}^2$  discussed above. Logically, except for the constant,  $\mathbf{b} = \mathbf{0}$  if and only if  $\mathbf{b}_s = \mathbf{0}$ . However, the Wald test on weight in the scaled regression indicates that weight is significant, while weight is not significant in the unscaled regression. Now, note that the test of significance of weight in the unscaled regression is obtainable as a nonlinear test on weight in the scaled regression.

Hence, the lack of invariance to scale in the Box–Cox regression model is just an example of the more general lack of invariance of Wald tests to nonlinear transformations.

## Scaling to elasticities

If all data were scaled in natural units, then there would be no issue here and researchers would always analyze data in their natural units. Of course, most data does not have any natural units and one scale is as arbitrary as another. Spitzer (1984) argues that the solution to the lack of invariance in the Box–Cox regression model is to always analyze data normalized by its geometric mean. The following example illustrates that if all data are scaled by their geometric means, then the coefficients on the independent variables from a left-hand-side only Box–Cox regression are like elasticities. Let G(x) be the geometric mean of x. The elasticity of the transformed dependent variable with respect to an independent variable evaluated at their geometric means would be

$$\frac{\frac{\partial y^{(\theta)}}{(G(y))^{(\theta)}}}{\frac{\partial x}{G(x)}} = \frac{\partial y^{(\theta)}}{\partial x} \frac{G(x)}{(G(y))^{(\theta)}}$$

Even with the data scaled as Spitzer suggests, this computation will not produce the coefficients on the independent variables in a left-hand-side only Box–Cox regression. The formula that will reproduce these coefficients is

$$\frac{\frac{\partial y^{(\theta)}}{\overline{G(y)^{\theta}}}}{\frac{\partial x}{\overline{G(x)}}} = \frac{\partial y^{(\theta)}}{\partial x} \frac{G(x)}{G(y)^{\theta}}$$

The denominators are the same in the two computations. The numerator in the first computation is the change in the transformed dependent variable as a fraction of the Box–Cox transformation of the geometric mean of the dependent variable. In the second case the numerator is the change in the transformed dependent variable as a fraction of the geometric mean of the dependent variable raised to power  $\theta$ . The former equation is an elasticity. The latter equation is "like" an elasticity and is what is produced by Spitzer's method.

Now let's use Stata to calculate these formulas and verify that when all variables are scaled by their geometric means a left-hand-side only Box-Cox regression produces coefficient estimates that are identical to those produced by the "like elasticity" formula. We begin by computing the geometric means of the variables of interest and saving them in scalars. Several functions of these means are also calculated. In particular, elw2 is the elasticity" computed by the formula given above. Note that they are not equal.

. box mpg (output om	weight price <i>nitted</i> )	, nolog			
. means mp	og				
Variable	Туре	Obs	Mean	[95% Conf.	Interval]
mpg	Arithmetic Geometric Harmonic	74 74 74	21.2973 20.58444 19.92318	19.9569 19.38034 18.81185	22.63769 21.86335 21.17405

. scalar mdot=r(mean\_g) /\* mdot is geometric mean of depvar \*/ . gen mpgs=mpg/r(mean\_g) /\* mpgs is scaled depvar \*/ . scalar mdot2=mdot^(\_b[theta: \_cons]) /\* this is denominator for like elasticity \*/ . scalar mdot2b=(mdot^(\_b[theta: \_cons])-1)/(\_b[theta: \_cons]) /\* This is denominator for elasticity \*/ . means weight Obs Variable Туре Mean [95% Conf. Interval] weight | Arithmetic 74 3019.459 74 2918 284 2839.398 3199.521 2743.65 3104.034 Geometric 74 2918.284 Harmonic 74 2816.578 2649.055 3006.719 . scalar wdot=r(mean\_g) /\* geometric mean of weight \*/ . gen weights=weight/r(mean\_g) /\* scaled weight \*/ . means price Variable | Type Obs Mean [95% Conf. Interval] price | Arithmetic 74 6165.257 5481.914 6848.6 | Geometric 74 5656.907 5165.664 6194.865 | Harmonic 74 5296.672 4928.901 5723.75 \_\_\_\_\_ ----+--. scalar pdot=r(mean\_g) /\* geometric mean of price \*/ . gen prices=price/r(mean\_g) /\* scaled price \*/ . scalar elw=\_b[ntrans: weight]\*wdot/mdot2 /\* apply like elasticity formula\*/ . di elw -.75713121 . scalar elw2=\_b[ntrans: weight]\*wdot/mdot2b /\* apply elasticity formula \*/ . di elw2 -.06463091 . scalar elp=\_b[ntrans: price]\*pdot/mdot2 /\* apply like elasticity formula\*/ . di elp -.07486248

Now we need to verify that when all the variables are scaled by their geometric means, the coefficients on the independent variables are identical to those computed using the "like elasticity" formula. Below is the output from a Box-Cox regression of mpgs = mpg/G(mpg) on weights = weight/G(weight) and prices = price/G(price).

```
    box mpgs prices weights, nolog
    Estimating comparison model
    Maximizing concentrated likelihood
    Maximizing the unconcentrated likelihood
```

				Numb	er of obs	=	74
				LR c	hi2(3)	=	100.40
Log likelih	hood = 45.7	16772		Prob	> chi2	=	0.0000
mpgs	Coef.	Std. Err.	z	P> z	[95% C	onf.	Interval]
ntrans							
prices	0748625	.0360538	-2.076	0.038	14552	67	0041983
weights	7571312	.0680234	-11.130	0.000	89045	47	6238077
_cons	.8398833	.0612024	13.723	0.000	.71992	87	.9598378
Ancillary							
theta	7568508	.2902995	-2.607	0.009	-1.3258	27	1878742
sigma	.1304014	.0107189	12.166	0.000	.10939	27	.1514101

Note that the coefficients on the independent variables are identical to those calculated by elw and elp above. These equalities illustrate the claim that when all the variables are scaled by their geometric means, the coefficients on the independent variables from a left-hand-side only Box–Cox regression are "like elasticities".

#### An LR test solution

Software developers must choose how to handle the manipulability issue. There are several options. One would be to automatically scale all the variables by their geometric mean and produce Wald tests of significance in a standard output table.

This alternative would force users interested in the coefficients expressed in another scale to transform them "by hand". The fact that the coefficient estimates are not true elasticities in all the Box–Cox models further reduces the appeal of this solution. Since likelihood-ratio tests are invariant to any rescaling of the variables there is another option. Allow users to run the regression in any scale desired but only perform likelihood-ratio tests as opposed to Wald tests. I chose the latter in constructing the new boxcox2. Users can estimate their models in the scale most convenient for them and easily obtain scale invariant test statistics.

The following example from the auto data using the new boxcox2 illustrates that LR statistics are invariant to the scale of the data.

. boxcox2 Estimating	mpg weight pr comparison n	rice , nolo; nodel	g nologlr lr	test		
Estimating	g IUII model g comparison g	nodels for	IR tosts			
Log likeli	hood = -178.0	06886		Number LR chi2 Prob >	of obs = (2) = chi2 =	74 100.40 0.000
mpg	Coef.	Std. Err.	z	P> z	[95% Conf.	Interval]
/theta	7568509	.2902995	-2.607	0.009		1878744
Estimates	of scale-var:	iant parame <sup>.</sup>	ters			
	Coef.	chi2(df)	P>chi2(df)	df of chi2		
Notrans   weight   price   _cons	0000263 -1.34e-06 1.272474	72.791 4.202	0.000 0.040	1 1		
/sigma	.0218107					
Test HO:	Restric log like	ted LR	statistic X~chi2	P-Value Pr > chi2		
theta = $-1$ theta = $0$ theta = $1$	-178.4: ) -181.4: 195.2:	1823 3399 1698	0.70 6.73 34.30	0.403 0.009 0.000		
. boxcox2 Estimating Estimating Estimating Log likeli	mpg2 weight p g comparison n g full model g comparison n hood = -7.67	orice , nol nodel nodels for : 75588	og nologlr 1 LR tests	rtest Number LR chi2 Prob >	of obs = (2) = chi2 =	74 100.40 0.000
mpg2	Coef.	Std. Err.	z	P> z	[95% Conf.	Interval]
/theta	7568511	.2902995	-2.607	0.009	-1.325828	1878745
Estimates	of scale-var:	iant parame <sup>.</sup>	ters			
	Coef.	chi2(df)	P>chi2(df)	df of chi2		
Notrans   weight   price   _cons	0001502 -7.66e-06 1.042532	72.791 4.202	0.000 0.040	1 1		
+ /sigma	.0869115					
Test HO:	Restric log like	cted LR Lihood	statistic X~chi2	P-Value Pr > chi2		
theta = $-1$ theta = $0$ theta = $1$	-8.0269 0 -11.042 -24.829	9351 2697 5684	0.70 6.73 34.30	0.403 0.009 0.000		

There are two important points to note about this output. First, the coefficient estimates exactly match those from the previous procedures. Second, the LR tests are invariant to changes in the scale of the transformed dependent variable.

#### Conclusion

This article has illustrated two important facts. First, the value of Wald tests of significance are not invariant to nonlinear transformations. Second, an important special case of this result is that Wald tests on the significance of an independent variable are not invariant to changes in the scale of any transformed variable in a Box–Cox regression model. This article has also illustrated that LR tests are invariant to the scale of transformed variables in a Box–Cox regression model. It has also argued that allowing researchers to choose their own scale for estimation with LR based inference is superior to boxing them into a specific scale that has some desirable properties.

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sg132	Analysis of variance from summary statistics

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Abstract: aovsum is a command for performing analysis of variance when the data are available only in summary form; namely, as group sizes, means, and standard deviations. This is accomplished by synthesizing a dataset to match those summary values. Other linear model style analyses can then be performed using the synthetic data; for example, multiple comparisons and trend analysis.

Keywords: ANOVA, univariate summary, linear model.

#### Introduction

It is common practice in many scientific journals to summarize data with a table showing, for various groups, the sample size (n), mean  $(\bar{y})$ , and standard deviation (s) for some collection of variables; possibly, the standard error  $s/\sqrt{n}$  appears in place of s. A reader might on occasion wish that the authors had also provided an analysis of variance (ANOVA) for some variable(s). That desire might spring from curiosity about the ANOVA F-statistic and its p-value, or from a need for the ANOVA's pooled estimate of error variance. Or, perhaps the groups in the table correspond to the cells of an unbalanced factorial design. To judge the size and significance of the various main and interaction effects from an inspection of a table of means and standard deviations can be a nontrivial task.

aovsum is a command that can compute the ANOVA summary table corresponding to a series of sample sizes, means, and standard deviations (or, standard errors). aovsum capitalizes upon some simple facts:

- 1. Any one-way ANOVA for independent groups can be computed from the values of n,  $\bar{y}$ , and s in the various groups.
- 2. Any multifactor design having only fixed factors can, without loss, be construed as a one-way design with K groups, where K is the total number of cells in the design. This tactic is the basis of the *cell means approach* to analyzing data from factorial designs.
- 3. Finally, let n > 0,  $\bar{y}$ , and s > 0 be given. Then a dataset consisting of n 1 copies of the value  $\bar{y} + s/\sqrt{n}$  and one copy of  $\bar{y} (n-1)s/\sqrt{n}$  will have mean equal to  $\bar{y}$  and standard deviation equal to s.

aovsum uses (3) to synthesize a dataset with the correct mean, standard deviation, and sample size in each of the various groups. aovsum then invokes oneway to present the one-way ANOVA for that synthetic dataset, in accord with (1). But aovsum can optionally save the synthetic data, and the user can then create variables that encode the factors of the underlying experimental design; the inverse of the tactic described in (2). The ANOVA command can then be used to examine the various main and interaction effects, as desired. The process is entirely accurate, subject only to limits imposed by the precision to which the means and standard deviations (or standard errors) have been reported. The only requirement is that the appropriate ANOVA model specify a single random term, as in fixed-effects, between-subject designs. For the sake of illustration, the examples below

are situations where the raw data are in fact available; in practice, of course, aovsum is useful only when the raw data are not available.

## Syntax

```
There are two forms of syntax:

aovsum , n(nlist) mean(mlist) { sd(SDlist) | se(SElist) } [names(yname [grpname [freqname]])

keep onewayopt ]

aovsum ?
```

## Description

In the first form, *nlist* is a list of sample sizes and *mlist* is a list of the associated sample means. *SDlist* and *SElist* are lists of sample standard deviations and standard errors, respectively; exactly one of *SDlist* and *SElist* is required.

The second form displays a terse reminder of the first form, by issuing the command which aovsum.

## Options

onewayopt is a string containing any of the options of the oneway command.

keep causes the synthetic data to be saved to three variables named (by default) y\_, cond\_, and freq\_. Without the keep option, the synthetic data are discarded after oneway finishes its work.

names provides alternatives for the three variable names to receive the synthetic data if the keep option is specified.

## Example 1

Consider an example having K = 4 groups with means and standard deviations given to three digit accuracy:

. aovsum, n(12	11 9 9) m(18.1	28.2 48.	3 70.2) sd(8.54	14.3 12.4	14.0)
Groups	Summary of R	esponse v	ariable		
(cells)	Mean S	td. Dev.	Obs.		
+					
1	18.1	8.54	12		
2	28.2	14.3	11		
3	48.3	12.4	9		
4	70.2	14	9		
Total	38.87561	23.29631	41		
Total	Analy	aia of Vo			
_	Апату	SIS OI VA	riance	_	
Source	SS	df	MS	F	Prob > F
Between groups	16063.495	6 3	5354.49854	35.09	0.0000
Within groups	5645.227	6 37	152.573719		
Total	21708.723	2 40	542.71808		
Bartlett's test	for equal var	iances:	chi2(3) = 2.98	876 Prob>	chi2 = 0.394

Retaining the synthetic data with keep enables several other possibilities. Prefacing aovsum with quietly will suppress the ANOVA output, useful when only the synthetic data are of interest.

. quietly aovsum, n(12 11 9 9) m(18.1 28.2 48.3 70.2) sd(8.54 14.3 12.4 14.0) keep . list freq\_ y\_ cond\_ freq\_ cond\_ 20.565286 1. 1 11 2. 10 32.511612 2 з. 8 52.433333 3 4. 74.866667 4 8 5. -9.0181421 1 6. -14.916122 2 1 7. 15.233333 3 1 8. 1 32.866667 4

Many standard analyses can be now performed by including the variable freq\_ as an fweight. Suppose, for example, that cond\_ is a so-called continuous variable, and that we wish to investigate a linear trend in the mean of the response variable.

Either the regress or the anova command could be used for that purpose, but first make a copy of the variable cond to permit a small trick with anova:

	gen byte Cond_ = cond_						
	** Test for linear trend	and deviation	from	linear tr	end:		
•	anova y_ cond_ Cond_ [fw	=freq_], cont(	cond_	) seq			
		Number of obs	=	41	R-squared	=	0.7400
		Root MSE	= 12	.3521	Adj R-squared	=	0.7189
	Source	Seq. SS	df	MS	F	Р	rob > F
	Model	16063.4956	3	5354.4985	4 35.09		0.0000
	cond_	15653.4326	1	15653.432	6 102.60		0.0000
	Cond_	410.063011	2	205.03150	6 1.34		0.2733
	Residual	5645.2276	37	152.57371	9		
	Total	21708.7232	40	542.7180	8		

The entry for cond\_ provides the usual ANOVA test for the linear contrast in the means of the response variable, while the Cond\_ entry gives the ANOVA test for deviation from linear trend in the means.

The means and standard deviations for this example were computed from individual data given in Table 12.11.1 of Snedecor and Cochran (1980); those data are included with this insert as ldose.dta. Their Table 12.11.2 gives the ANOVA summary table, and their Table 12.11.3 gives the test for linear trend and deviation from linearity. The output from aovsum and anova shown above may be compared with those tables. Alternatively, "exact" results for the trend analysis tests can be obtained thus:

```
use ldose, clear
(Snedecor & Cochran Table 12.11.1)
. describe
Contains data from ldose.dta
                                      Snedecor & Cochran Table 12.11.1
 obs:
              41
                                      3 Jan 2000 13:32
vars:
               2
             246 (95.5% of memory free)
size:
_____
            _____
             byte
                  %8.0g
                                      Lethal dose (minus 50 units)
  1. ldose
  2. rate
             byte
                 %8.0g
                                      Injection rate,
                                      (mg/kg/min)/1045.75
                                                      _____
Sorted by:
 ** Create a copy of the group variable, again:
. gen byte Rate = rate
. ** And run -anova-, again:
. anova ldose rate Rate, cont(rate) seq
                      Number of obs = 41
                                             R-squared
                                                       = 0.7402
                      Root MSE = 12.3574
                                            Adj R-squared = 0.7191
              Source | Seq. SS
                                df MS
                                             F Prob > F
                       _____
               Model | 16094.2817 3 5364.76055
                                                 35.13
                                                           0.0000
                                   1 15683.5493
                                                  102.70
                rate
                       15683.5493
                                                           0.0000
                       410.732323 2 205.366162
                                                  1.34
                                                           0.2730
                Rate
             Residual | 5650.10859 37 152.705637
               Total | 21744.3902 40 543.609756
```

## Example 2

Here, aovsum will silently create three new variables, days, group, and freq.:

. quietly aovsum, n(13 14 20 26 20 20 16 17) /\*
> \*/ m(13.62 15.79 16.55 7.00 31.75 10.45 20.06 19.18) /\*
> \*/ sd(12.07 17.49 14.75 6.11 22.07 10.68 14.22 17.90) /\*
> \*/ keep names(days group)

There are eight groups of Australian children and the response variable is days absent from school. The means and standard deviations were computed from Table 4 of Paul and Banerjee (1998), a set of data originally collected by Quine (1975). The groups form a 2 (race)  $\times$  4 (grade in school) cross-classification. Variables encoding those two factors could be entered in Stata's data editor, or created with code resembling

```
. gen byte race = mod(group-1, 2)
. gen byte grade = int((group-1)/2)
```

Then, the usual two-way ANOVA of the response variable can be computed as

. ano	va day	s race	grade ra	ce*grade [fw=f]	req_]			
				Number of obs	-	146	R-squared	= 0.2120
				Root MSE	= 14	.8357	Adj R-squared	= 0.1720
			Source	Partial SS	df	MS	F	Prob > F
			Model	8169.29067	7	1167.041	52 5.30	0.0000
			race	1907.27695	1	1907.2769	95 8.67	0.0038
			grade	2259.47976	3	753.15992	21 3.42	0.0191
		rac	e*grade	2896.15272	3	965.38423	39 4.39	0.0056
		R	esidual	30373.3948	138	220.09706	34	
			Total	38542.6855	145	265.81162	24	

Quine's (1975) raw data are included as absences.dta; the "exact" two-way ANOVA is thus:

. . .

```
use absences, replace
(Quine's School Absences Data)
. describe
Contains data from absences.dta
 obs:
               146
                                           Quine's School Absences Data
vars:
                  4
                                           3 Jan 2000 12:42
             1,168 (95.2% of memory free)
                                          (_dta has notes)
size:
                         ------
_____
                                                               _____
                     %8.0g
  1. davs
              byte
                                           Davs absent from school
                                           Race x Grade group
  2. group
               byte
                     %8.0g
  3. race
               byte
                     %8.0g
                                race
                                           Race of child
  4. grade
               byte
                     %9.0g
                                 grade
                                           Grade in school
```

Sorted by:

. \*\* And the ANOVA:

. anova days race grade race\*grade

Number of obs = 146 R-squared = 0.2119= 14.8369 Root MSE Adj R-squared = 0.1720MS Source | Partial SS df F Prob > F Model | 8169.67223 7 1167.09603 5.30 0.0000 1908.01254 1 1908.01254 8.67 0.0038 race grade 2259.85192 3 753.283973 3.42 0.0191 0.0056 2895.42955 3 965.143183 race\*grade 4.38 Residual | 30378.4922 138 220.134001 Total | 38548.1644 145 265.84941

## **Saved Results**

After a call to aovsum, the contents of r() will be the same as following a call to oneway with the options specified in *onewayopt*.

#### References

Paul, S. R. and T. Banerjee. 1998. Analysis of two-way layout of count data involving multiple counts per cell. Journal of the American Statistical Association 93: 1419–1429.

Quine, S. 1975. Unpublished Ph.D. thesis, Australian National University.

Snedecor, G. W. and W. G. Cochran. 1980. Statistical Methods. 7th ed. Ames, IA: Iowa State University Press.

sg133 Sequential and drop one term likelihood-ratio tests	
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Abstract: Commands extending Stata's lrtest command are given for likelihood-ratio tests after maximum likelihood estimation. **Keywords:** Likelihood-ratio tests, Akaike information criterion, AIC.

#### Syntax

lrseq [, fp(format) fchi(format) ]
lrdrop1 [, fp(format) fchi(format) ]

## Description

This insert includes two commands: lrdrop1 and lrseq. Both commands perform likelihood-ratio tests after maximum likelihood estimations such as those by stcox, logit, logistic, poisson, and so on. They are extensions of the Stata command lrtest.

The lrseq command is designed to perform sequential pairwise likelihood-ratio tests. It starts with a null model. Explanatory variables are added into the model sequentially. At each step, the current model is compared with the previous one. The lrdrop1 command performs likelihood ratio tests after dropping terms from the original model one at a time in turn, comparing each new model with the original model. Both commands report the Akaike information criterion (AIC) developed by Akaike (1974). For a model having r parameters,

 $AIC = -2\log(likelihood) + 2r$ 

Analysts can use these two commands to select models interactively. Alternatively, the command swaic (see Wang 2000) can be used for an automatic model selection using AIC. Another relevant command is lrtest2 introduced by Perez-Hoyos and Tobias (1999).

## Options

fp(format) specifies the output format for p-values with default value %9.4f.

fchi(format) specifies the output format for chi2 values, with default value %9.2f.

## **Examples**

We begin with a call to logit:

. xi: logit i.expose	; outcome age	e sex i.expos Iexpos_1-3	se hibp bmi (naturally	., nolog v coded; Iex	pos_1 om	itteo	d)
Logit estim	nates			Number	of obs	=	399
•				LR chi	2(6)	=	42.13
				Prob >	chi2	=	0.0000
Log likelih	100d = -104	.4184		Pseudo	0 R2	=	0.1679
outcome	Coef.	Std. Err.	Z	P> z	[95% C	onf.	Interval]
age	.0349601	.0157084	2.226	0.026	.00417	21	.065748
sex	.390423	.3878383	1.007	0.314	3697	26	1.150572
Iexpos_2	1.333849	.6090427	2.190	0.029	.14014	77	2.527551
Iexpos_3	2.601842	.5930699	4.387	0.000	1.4394	46	3.764237
hibp	.0042039	.3858058	0.011	0.991	75196	516	.7603694
bmi	1136088	.0425776	-2.668	0.008	19705	94	0301582
_cons	-2.749143	1.460547	-1.882	0.060	-5.6117	63	.1134774

Now we use lrdrop1:

outcome	Df	Chi2	P>Chi2	-2*log 11	Res. Df	AIC
Uriginal M	odel			208.84	392	222.84
-age	1	5.12	0.0237	213.95	391	225.95
-sex	1	1.02	0.3123	209.86	391	221.86
-lexpos*	2	27.67	0.0000	236.51	390	246.51
-hibp	1	0.00	0.9913	208.84	391	220.84
-bmi	1	8.11	0.0044	216.95	391	228.95

. lrseq Sequential logit regre number of o	Likelik ssion bs = 39	nood Ratio 99	Tests			
outcome	Df	Chi2	P>Chi2	-2*log ll	Res. Df	AIC
Null Model				250.96	398	252.96
age	1	9.34	0.0022	241.62	397	245.62
sex	1	0.36	0.5480	241.26	396	247.26
Iexpos*	2	24.32	0.0000	216.95	394	226.95
hibp	1	0.00	0.9859	216.95	393	228.95
bmi	1	8.11	0.0044	208.84	392	222.84

Terms added sequentially (first to last)

One lrseq or lrdrop1 command in this example is equivalent to performing lrtest five times. The likelihood-ratio test for variable sex in the lrseq output; for example, compares a model with age and sex against a model with only age. Iexpos\* is for the categorical variable expose with three categories and two degrees of freedom.

## Acknowledgments

I thank Dr. John L. Moran, Queen Elizabeth Hospital, Adelaide, Australia for useful suggestions and Dr. Wendy Hoy, Menzies School of Health Research, Darwin, Australia for providing the example data.

#### References

Akaike, H. 1974. A new look at statistical model identification. *IEEE Transactions on Automatic Control* AC-19: 716-723. Perez-Hoyos, S. and A. Tobias. 1999. sg111: A modified likelihood-ratio test command. *Stata Technical Bulletin* 49: 24–25. Wang, Z. 2000. sg134: Model selection using the Akaike information criterion. *Stata Technical Bulletin* 54: 47–49.

sg134	Model selection using the Akaike information criterion

Zhiqiang Wang, Menzies School of Health Research, Darwin, Australia, wang@menzies.edu.au Abstract: A command for performing stepwise model selection using the Akaike information criterion is described and illustrated. Keywords: Stepwise model selection, Akaike information criterion, AIC.

## Syntax

swaic [, fp(format) fchi(format) back model ]

## Description

The command swaic in this insert is designed to perform stepwise model selection using the Akaike Information Criterion (AIC) developed by Akaike (1974) after maximum likelihood estimation. For a model having r parameters,

 $AIC = -2 \log(likelihood) + 2r$ 

It is an alternative approach to stepwise model selection in Stata. swaic starts with a null or full model. It takes a step by adding or dropping a term that produces the minimum AIC. swaic reports likelihood ratio tests as well as AIC values for all steps. With the model option, swaic reports the final model with the minimum AIC value. The current version of swaic works with logit, logistic, stcox, poisson, probit, and streg.

## Options

fp(format) specifies the output format for p-values, with default value %9.4f.

fchi(format) specifies the output format for chi2 values, with default value %9.2f.

back uses a backward method starting with a full model, the default is a forward method.

model reports a final model having the minimum AIC value.

#### Example

We illustrate swaic by first using logit and then using swaic with the model option:

. xi: log i.expose	it outcom	e age I	sex i.exp expos_1-3	ose hibp b (natural)	ni, nolog Ly coded;	g Iexpos_	1 omitted	1)
Logit est	imates				- N1	mber of	obs =	399
TOBIO ODO	Indeed				LF	chi2(6)	=	42.13
					Pr	ob > chi	2 =	0.0000
Log likel	ihood =	-104.	4184		Ps	seudo R2	=	0.1679
outcome	Co	ef.	Std. Err.	z	P> z	[9	5% Conf.	Interval]
age	.0349	601	.0157084	2.226	0.026	.0	041721	.065748
sex	.390	423	.3878383	1.007	0.314		369726	1.150572
Iexpos_2	1.333	849	.6090427	2.190	0.029	.1	401477	2.527551
Iexpos_3	2.601	842	.5930699	4.387	0.000	1.	439446	3.764237
hibp	.0042	039	.3858058	0.011	0.991	7	519616	.7603694
bmi	1136	880	.0425776	-2.668	0.008	1	970594	0301582
_cons	-2.749	143	1.460547	-1.882	0.060	-5.	611763	.1134774
logit reg number of outcome	ression obs = 39	9  Df	Chi2	 P>Chi2		Df Res.	AIC	
Null Mode	-				250.96	398	252.96	
Step 1:	lexpos*	2	22.91	0.0000	228.06	396	234.06	
Step 2:	bmi	1	13.27	0.0003	214.79	395	222.79	
Step 3:	age	1	4.85	0.0276	209.94	394	219.94	
Step 4:	sex	1	1.10	0.2934	208.84	393	220.84	
Step 5:	птр		0.00	0.9913	208.84		222.84	
Logit est	imates				Nu	umber of	obs =	399
					LF	l chi2(4)	=	41.02
					Pr	cob > chi	2 =	0.0000
Log likel	ihood = -	104.9	7047		Ps	seudo R2	=	0.1635
outcome	Co	ef.	Std. Err.	z	P> z	[9	5% Conf.	Interval]
Iexpos_2	1.293	822	.5981625	2.163	0.031	.1	214446	2.466199
Iexpos_3	2.535	178	.580218	4.369	0.000	1.	397971	3.672384
bmi	1072	528	.0412597	-2.599	0.009	1	881203	0263853
age	.0338	024	.0156032	2.166	0.030	.0	032206	.0643842
_cons	-2.608	527	1.449736	-1.799	0.072	-5.	449958	.2329043

Then we use both the model and back options:

. swaic, m Stepwise M logit regr number of	nodel bac] Model Sele ression obs = 399	k ectio 9	n by AIC					
outcome		Df	Chi2	P>Chi2	-2*11	Df Res.	AIC	
Full Model	L				208.84	392	222.84	
Step 1:	-hibp	1	0.00	0.9913	208.84	393	220.84	
Step 2:	-sex	1	1.10	0.2934	209.94	394	219.94	
Step 3:	-age	1	4.85	0.0276	214.79	395	222.79	
Step 4:	-bmi	1	13.27	0.0003	228.06	396	234.06	
Step 5: -1	[expos*	2	22.91	0.0000	250.96	398	252.96	
Logit esti	imates				N	umber of ol	os =	399
					L	R chi2(4)	=	41.02
					Ρ:	rob > chi2	=	0.0000
Log likeli	ihood = -:	104.9	7047		P	seudo R2	=	0.1635
outcome	Coe	ef.	Std. Err.	z	P> z	[95]	Conf.	Interval]
age	.0338	024	.0156032	2.166	0.030	.00:	32206	.0643842
Iexpos_2	1.293	822	.5981625	2.163	0.031	.12	L4446	2.466199
Iexpos_3	2.535	178	.580218	4.369	0.000	1.39	97971	3.672384
bmi	1072	528	.0412597	-2.599	0.009	188	31203	0263853
_cons	-2.608	527	1.449736	-1.799	0.072	-5.44	19958	.2329043

Both backward and forward methods produce the same results in this example. The AIC reaches a minimum of 219.94 when the model only includes age, bmi and expose.

#### Acknowledgments

Thanks to Dr. John L. Moran, Queen Elizabeth Hospital, Adelaide, Australia for testing and comments and Dr. Wendy Hoy of the Menzies School of Health Research in Darwin, Australia for providing examples.

#### Reference

Akaike, H. 1974. A new look at statistical model identification. IEEE Transactions on Automatic Control, AC-19: 716-723.

sxd1.2 Random allocation of treatments balanced in blocks: update
---

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Abstract: Allocation of treatments to subjects using a random method underpins the validity of a clinical trial. Blocking is a technique that helps ensure a constant ratio of treatment allocations is maintained throughout the randomization period. ralloc facilitates blocked randomization in a variety of experimental designs including stratified, factorial, and crossover designs. Output may be configured in several ways to suit central or distributed randomization, and to facilitate the pharmacy preparing blocks of treatments.

Keywords: Experimental design, randomized controlled trials, randomization, blocking.

## Introduction

I have again updated the program ralloc, first described in Ryan (1998) and updated in Ryan (1999). The full syntax is ralloc *BlockIdvar BlockSizevar Treatmentvar*, saving(*filename*) [ { multif | nomultif } seed(#)

```
nsubj(#) ntreat(2|3|4) ratio(1|2|3) osize(1|2|3|4|5|6|7) init(#) { equal | noequal }
strata(#) using(filename) countv(varname) { tables | notables } trtlab(label1 [label2 ...])
matsiz(#) fratio( 1 1 | 2 1 | 1 2 | 2 2 ) factor(2*2|2*3|3*2|3*3|2*4|4*2|3*4|4*3)
xover({ stand | switch | extra }) shape({ long | wide }) ]
```

## STB-54

## **New Features**

The version of ralloc accompanying this insert has the following new features:

- 1. The second syntax displays the first syntax on screen.
- 2. The program supports stratified randomization.
- 3. The program supports two-treatment factorial designs.
- 4. The program supports a  $2 \times 2$  crossover design with or without either a "switchback" or "extra-period" of treatment in a third period as described by Jones and Kenward (1989).
- 5. A new, more efficient treatment labeling option is used.
- 6. The display of informative tables is now optional.

## **New options**

multif specifies that, for a stratified design, one file will be saved for the allocations in each stratum, in addition to a file storing all allocations. The *filename* specified in the saving option will be used as a stub to name the files according to the following schema

<filename>\_n1[\_n2\_n3 ... \_nk]

for a trial with 1 to k stratification variables. n1 identifies the level of the stratum of the 1st stratification variable, n2 gives the level of the stratum of the 2nd stratification variable, and so on, each stratification variable's set of suffixes being preceded by an underscore character. Suffixes are padded with leading zeros to maintain alphanumeric sort order. The default is nomultif.

- strata(#) specifies the number of strata and may be calculated as the product, over all stratifying variables, of the number of levels in each variable. A new variable, StratID, denoting the stratum identifier, is generated. The default is strata(1). strata is overridden by the specification of a using file.
- using(filename) names a file whose data define the stratification schema. The file must consist solely of variables defining strata plus one other variable giving the number of subjects required to be randomized in each stratum (the countv variable, see below). Each row (observation) of the file defines a stratum. Levels of a stratification variable must be coded as consecutive positive integers (1, 2, 3, ...). ralloc will check this and will also check that the product of levels over all stratification variables equals the number of rows (strata). Whether strata are defined by strata or by the rows of a using file, the number of strata cannot exceed 800.
- countv(varname) specifies the variable in the using file whose values give the number of subjects requiring randomization in each stratum. countv is specified if and only if a using file is specified. Values of countv override the value of nsubj should this also be specified.
- tables specifies that a frequency distribution of block sizes is displayed for all allocations and, where appropriate, for each stratum. The default is notables.
- trtlab(label1 [label2 ...]) allows specification of value labels for treatments. At most four labels may be specified for a nonfactorial design. The number of labels that may be specified for a factorial design is equal to the sum of the number of possible treatments in the two randomization axes. Labels are separated by spaces and so may not themselves contain a space. A label will be truncated after the first eight characters. The default treatment labels are A, B, C and D (plus E, F and G if required for a factorial design). An older form of the syntax for nonfactorial designs, requiring an option for each label by trllab(label), tr2lab(label), and so on, is permitted but obsolete.
- matsiz(#) sets the maximum size of a Stata matrix. This is a rarely used option, as ralloc chooses a matrix size appropriate to the stratification schema specified.
- fratio(*string*) specifies, in the case of a  $2 \times 2$  factorial design, the ratio of allocations in each axis. The string must be one of the choices given in the syntax diagram. For example, if we require a 1:2 ratio of treatments in the first randomization axis and a 1:1 ratio of treatments in the second axis, fratio(2 1) would be specified.
- factor(string) specifies that the trial has a factorial design with two "axes of randomization". The string must be one of the choices in the syntax diagram. Allocation combinations are balanced within blocks, unless fratio is specified in a  $2 \times 2$  design. The names of the two treatment variables generated will be the name specified by *Treatmentvar* followed by a 1 and a 2.

## Example 1

To illustrate the new trtlab, strata and multif options, we have

. ralloc blknum blksiz Rx, ns(494) osiz(2) eq ntreat(2) sav(mywide)
> shap(wide) trtlab(Placebo Active) strata(4) multif

which results in the allocation of two treatments labeled "Placebo" and "Active" equally in two block sizes, 2 and 4, to 494 subjects in each of four strata (maybe a four-center trial). Data are saved in wide form to five files: mywide.dta holds all allocations, and four additional files named mywide\_1.dta, mywide\_2.dta, mywide\_3.dta and mywide\_4.dta hold stratum specific allocations.

. use my . li in	wide_4 1/7, noobs	nodisp				
StratID	blknum	blksiz	Rx1	Rx2	Rx3	Rx4
4	498	2	Active	Placebo		
4	499	2	Placebo	Active		
4	500	2	Placebo	Active		
4	501	4	Placebo	Placebo	Active	Active
4	502	2	Placebo	Active		
4	503	2	Placebo	Active		
4	504	2	Active	Placebo		

## Example 2

To illustrate the using option, we have a file, raltest6.dta, defining strata for an RCT to be conducted in 3 centers. We also seek to balance allocations within two age groups. The required numbers of allocations in each of the  $3 \times 2 = 6$  strata are given by the variable freq.

•	use	raltest6		
	list	t		
		centre	freq	agegrp
	1.	1	50	1
	2.	1	80	2
	з.	2	140	1
	4.	2	100	2
	5.	3	70	1
	6.	3	100	2

Note that ralloc does not care about the order of variables in the data, nor of the sort order of the observations, but it is easier to check the completeness of the schema if levels are coherently nested. The command

. ralloc bID bsiz trt, sav(myrct) count(freq) using(raltest6)
> nsubj(80) seed(54109) multif

results in the generation of seven files. Note that the option nusbj(80) will be overridden by the values of freq in raltest.dta. After some informative output (not shown here), the data are written to the appropriate stratum-specific files and the file with all allocations, myrct.dta, is in memory. The stratum identifying variables have also been written to the datasets.

. li in 1/	8, noob noo	dis				
StratID	centre	agegrp	bID	bsiz	SeqInBlk	trt
1	1	1	1	2	- 1	Α
1	1	1	1	2	2	В
1	1	1	2	8	1	A
1	1	1	2	8	2	В
1	1	1	2	8	3	В
1	1	1	2	8	4	В
1	1	1	2	8	5	A
1	1	1	2	8	6	A

## Example 3

Consider a study that aims to test both the efficacy of a blood pressure lowering medication, called BPzap, versus a placebo, and the utility of two weight reduction exercise programs, called GymSweat and JogaBit, versus normal activity, on a specified cardiovascular endpoint. An efficient design might be a  $2 \times 3$  factorial RCT. The command

```
. ralloc blknum size Rx, sav(rctfact) factor(2*3) osiz(2) eq
> seed(4512) trtlab(BPzap Placebo GymSweat JogaBit normact)
> nsubj(300)
```

will allocate two treatments, called Rx1 and Rx2, to each of 300 subjects in a single stratum using a  $2 \times 3$  factorial design. Blocks of size 6 and 12 with equal frequency will result.

. list in 1	./10					
Stra	t ID	blknum	size	SeqInBlk	Rx1	Rx2
1.	1	1	6	- 1	Placebo	GymSweat
2.	1	1	6	2	BPzap	normact
3.	1	1	6	3	BPzap	GymSweat
4.	1	1	6	4	Placebo	normact
5.	1	1	6	5	BPzap	JogaBit
6.	1	1	6	6	Placebo	JogaBit
7.	1	2	12	1	BPzap	JogaBit
8.	1	2	12	2	BPzap	GymSweat
9.	1	2	12	3	BPzap	normact
10.	1	2	12	4	Placebo	JogaBit
. tab Rx1 R	lx2					
	1		Rx2			
Rx1	Gym	Sweat	JogaBit	normact	Total	
BPzap	- 	50	50	50	150	
Placebo	1	50	50	50	150	
Total	+	100	100	100	300	

and we note the balance in allocations in each axis of the study.

## Example 4

We reformulate the preceding study as a  $2 \times 2$  factorial design by excluding the JogaBit treatment. Let's say we wish to have twice as many on Placebo as BPzap, and also twice as many subjects on normal activity as on the GymSweat regimen.

```
. ralloc blknum size Rx, sav(rctfact2) factor(2*2) osiz(2) eq
> seed(1131) trtlab(BPzap Placebo GymSweat normact) fratio(2 2)
```

```
> nsubj(300)
```

- . . . . . . . .

This command will give blocks of sizes 9 (the minimum possible with 1:2 allocation ratios in each axis) and 18 (because osize(2) was specified).

. tab Rx\* Rx2 Rx1 GymSweat normact Total BPzap 68 102 34 Placebo 68 136 204 Total 102 204 306

## Example 5

We have a  $2 \times 2$  crossover design supplemented by a switchback in period 3. The trial compares a new antiarthritic drug "HipLube" versus aspirin in chronic osteoarthritis of the hip.

. ralloc Bnum Bsize medic, saving(chronOA) ns(28) osiz(1) init(4)
> trtlab(HipLube aspirin) xover(switch) strata(2)

medic1, medic2, and medic3 store the treatments administered in periods 1, 2 and 3 respectively:

. li in 1/6, noobs nodisp

${\tt StratID}$	Bnum	Bsize	SeqInBlk	medic1	medic2	medic3
1	1	4	1	HipLube	aspirin	HipLube
1	1	4	2	aspirin	HipLube	aspirin
1	1	4	3	HipLube	aspirin	HipLube
1	1	4	4	aspirin	HipLube	aspirin
1	2	4	1	HipLube	aspirin	HipLube
1	2	4	2	HipLube	aspirin	HipLube

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## References

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-----. 1999. Update to random allocation of treatments in blocks. Stata Technical Bulletin 50: 36-37.

## STB categories and insert codes

Inserts in the STB are presently categorized as follows:

Gene	ral Categories:		
an	announcements	ip	instruction on programming
сс	communications & letters	OS	operating system, hardware, &
dm	data management		interprogram communication
dt	datasets	qs	questions and suggestions
gr	graphics	tt	teaching
in	instruction	ZZ	not elsewhere classified
Statis	tical Categories:		
sbe	biostatistics & epidemiology	ssa	survival analysis
sed	exploratory data analysis	ssi	simulation & random numbers
sg	general statistics	SSS	social science & psychometrics
smv	multivariate analysis	sts	time-series, econometrics
snp	nonparametric methods	svy	survey sampling
sqc	quality control	sxd	experimental design
sqv	analysis of qualitative variables	SZZ	not elsewhere classified
srd	robust methods & statistical diagnostics		

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- 1. An insert (article) describing the purpose of the submission. The STB is produced using plain T<sub>F</sub>X so submissions using TEX (or LATEX) are the easiest for the editor to handle, but any word processor is appropriate. If you are not using TEX and your insert contains a significant amount of mathematics, please FAX (979-845-3144) a copy of the insert so we can see the intended appearance of the text.
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